

Sensitivity analysis

Andrea Saltelli Centre for the Study of the Sciences and the Humanities, University of Bergen, and Open Evidence Research, Open University of Catalonia; August 27th–September 1st, 2018, Course Numbers for policy, Castelldefels (Barcelona)



Where to find this talk: www.andreasaltelli.eu



Blurring lines:

"what qualities are specific to rankings, or indicators, or models, or algorithms?"

E. Popp Berman and D. Hirschman, The Sociology of Quantification: Where Are We Now?, Contemp. Sociol., vol. in press, 2017.

"[in climate modelling] it looks very little like our idealized image of science, in which pure theory is tested with pure data.

[impossible to] eliminate the modeldependency of data or the data-ladenness of models"

Paul N. Edwards, 1999, Global climate science, uncertainty and politics: Data-laden models, model-filtered data.

"[For] philosophers Frederick Suppe and Stephen Norton the blurry model/data relationship pervades all science"

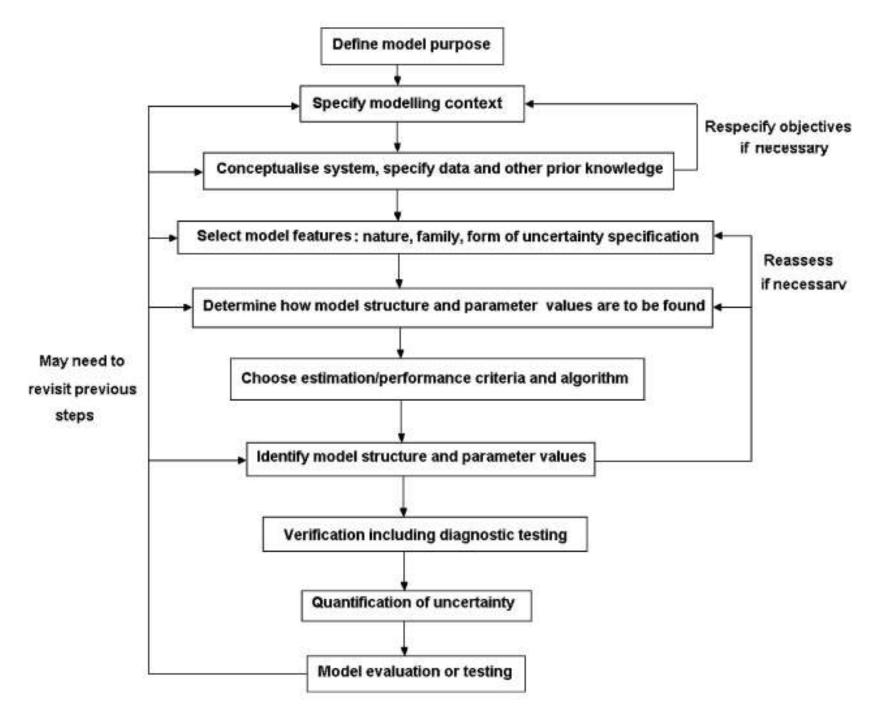
Paul N. Edwards, 1999, Global climate science, uncertainty and politics: Data-laden models, model-filtered data. Padilla et al. call for a more structured, generalized and standardized approach to verification

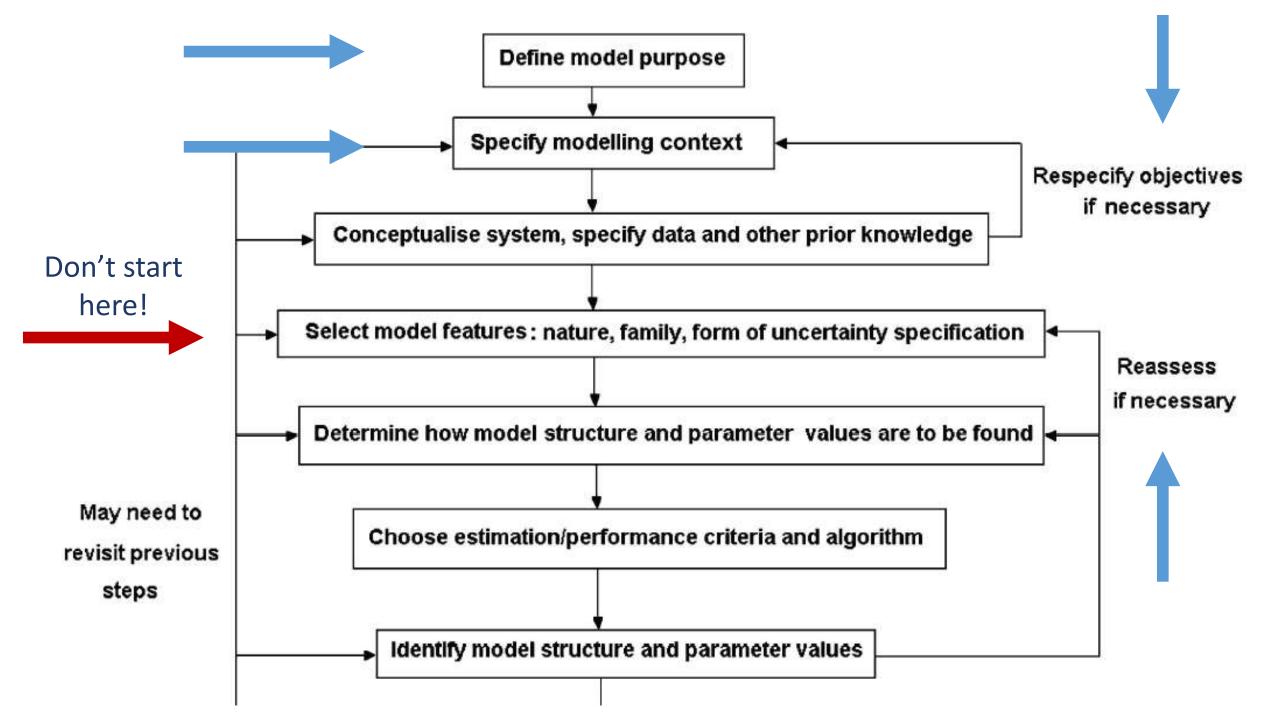
Jakeman et al. call for a 10 points participatory checklist including NUSAP and J. R. Ravetz's process based approach

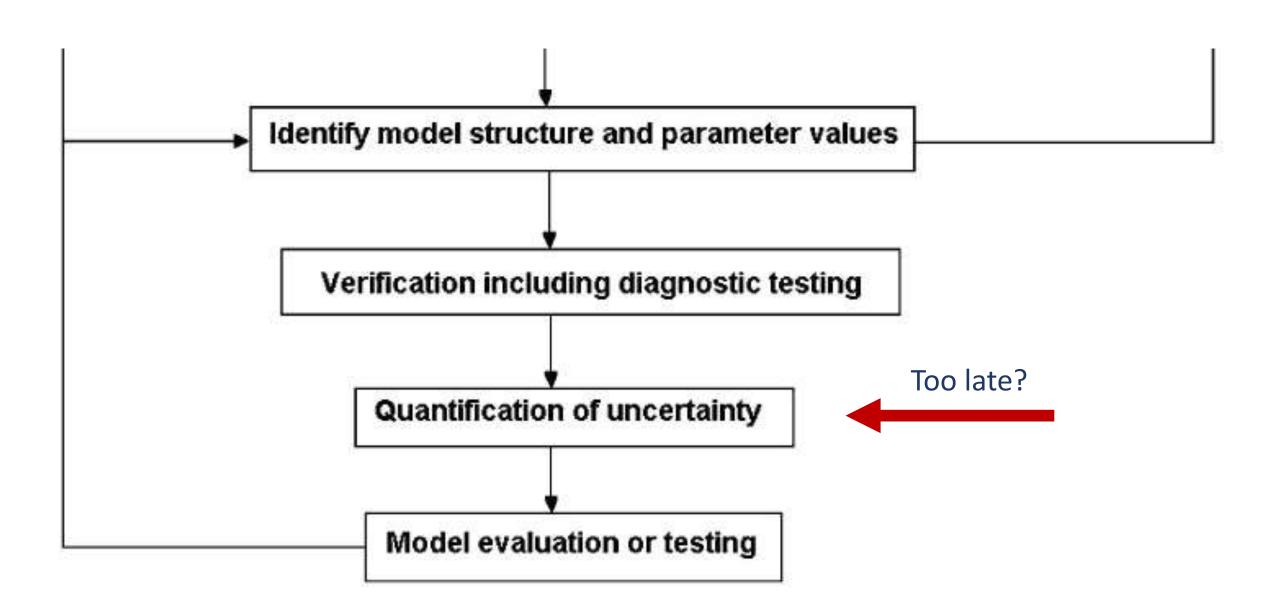
For NUSAP: Funtowicz, S.O., Ravetz, J.R., 1990. Uncertainty and Quality in Science and Policy. Kluwer, Dordrecht

J. R. Ravetz, "Integrated Environmental Assessment Forum, developing guidelines for 'good practice', Project ULYSSES.," 1997.http://www.jvds.nl/ulysses/eWP97-1.pdf









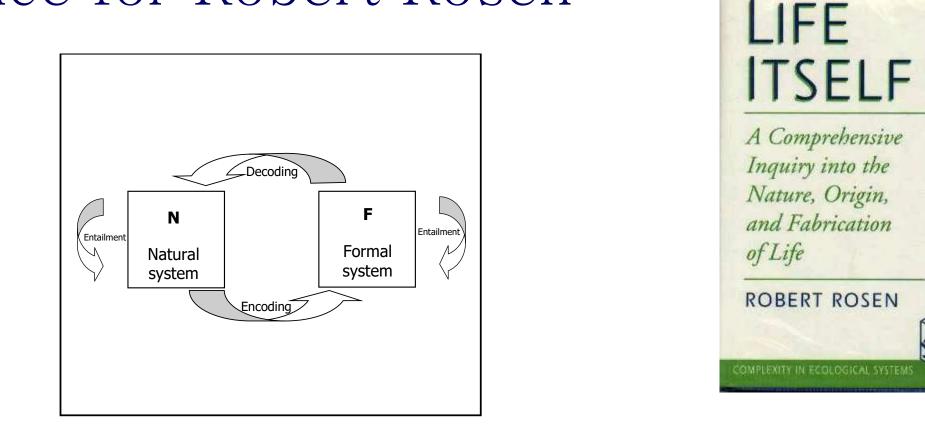
Not a discipline

Unlike statistics, mathematical modelling is not a discipline, hence the lack of universally accepted quality standards, disciplinary fora and journals and recognized leaders

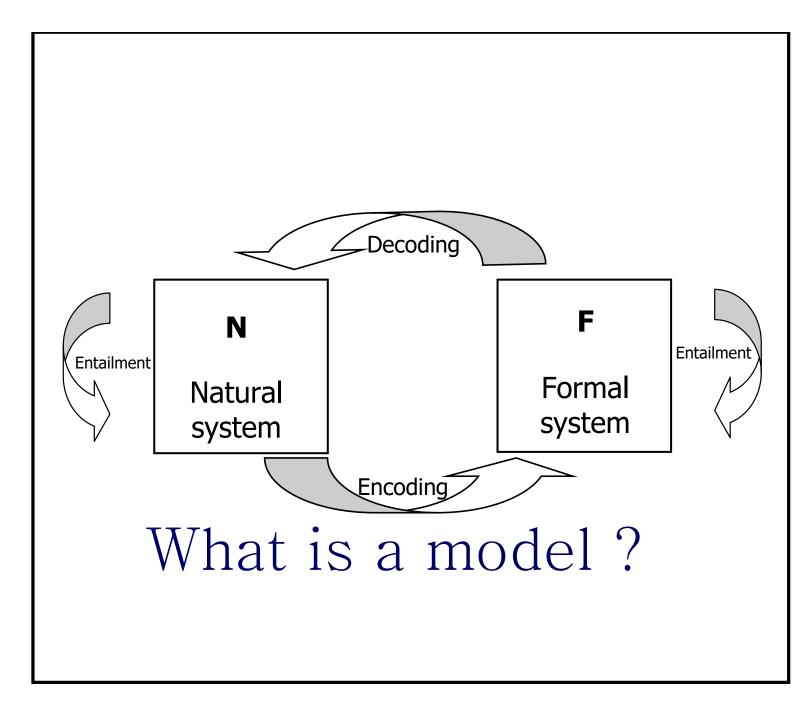
Making sensitivity analysis part of the syllabus of statistics?

Saltelli, A., Does Modelling need a reformation? Ideas for a new grammar of modelling, available at https://arxiv.org/abs/1712.06457

Modelling as a craft rather than as a science for Robert Rosen



R. Rosen, Life Itself: A Comprehensive Inquiry Into the Nature, Origin, and Fabrication of Life. Columbia University Press, 1991.





Robert Rosen

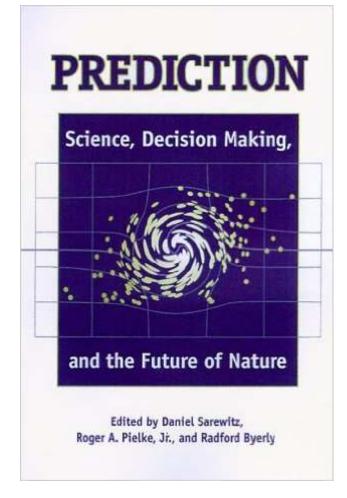
"models are most useful when they are used to challenge existing formulations, rather than to validate or verify them"



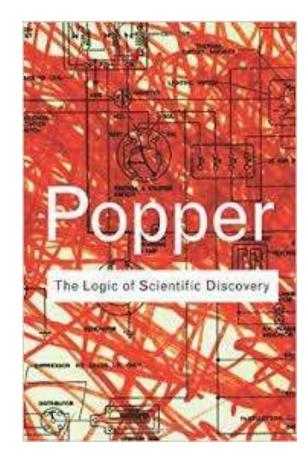
Naomi Oreskes

N. Oreskes, K. Shrader-Frechette, and K. Belitz, "Verification, Validation, and Confirmation of Numerical Models in the Earth Sciences," Science, 263, no. 5147, 1994.

Models are not physical laws



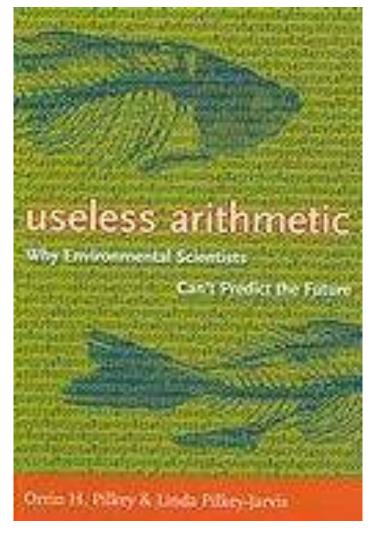
Oreskes, N., 2000, Why predict? Historical perspectives on prediction in Earth Science, in Prediction, Science, Decision Making and the future of Nature, Sarewitz et al., Eds., Island Press, Washington DC "[…] to be of value in theory testing, the predictions involved must be capable of refuting the theory that generated them" (N. Oreskes)



"In many cases, these temporal predictions are treated with the same **respect** that the hypothetic-deductive model of science accords to logical predictions. But this respect is largely misplaced"

"[…] models are complex amalgam of theoretical and phenomenological laws (and the governing equations and algorithms that represent them), empirical input parameters, and a model conceptualization [...] When a model generates a prediction, of what precisely is the prediction a test? The laws? The input data? The conceptualization? Any part (or several parts) of the model might be in error, and there is no simple way to determine which one it is"

Egregious modelling failure from Pilkey and Pilkey–Jarvis (from AIDS to coastal erosion to nuclear waste disposal ...)



O. H. Pilkey and L. Pilkey-Jarvis, Useless Arithmetic: Why Environmental Scientists Can't Predict the Future. Columbia University Press, 2009.

For John Kay modelling may need as input information which we don't have (The case of WEBTAG; knowing car passengers number decades into futures)

John Kay

J. A. Kay, "Knowing when we don't know," 2012, https://www.ifs.org.uk/docs/john_kay_feb2012.pdf



WebTAG: Annual Percentage Change in Car Occupancy (% pa) up to 2036

| Journey Purpose | Weekday | | | | | | |
|--|--------------|--------------|---------|---------|--------------------|---------|----------|
| | 7am- 10am | 10am- 4pm | 4pm-7pm | 7pm-7am | Weekday Average | Weekend | All Week |
| Work | -0.48 | -0.4 | -0.62 | -0.5 | -0.44 | -0.48 | -0.45 |
| Non - Work (commuting and other) | -0.67 | -0.65 | -0.53 | -0.47 | -0.59 | -0.52 | -0.56 |

Economics

Paul Romer's Mathiness = use of mathematics to veil normative stances

Erik Reinert: scholastic tendencies in the mathematization of economics

P. M. Romer, "Mathiness in the Theory of Economic Growth," Am. Econ. Rev., vol. 105, no. 5, pp. 89–93, May 2015.

E. S. Reinert, "Full circle: economics from scholasticism through innovation and back into mathematical scholasticism," J. Econ. Stud., vol. 27, no. 4/5, pp. 364–376, Aug. 2000.

Uncertainty and sensitivity analysis

Definitions

Uncertainty analysis: Focuses on just quantifying the uncertainty in model output

Sensitivity analysis: The study of the relative importance of different input factors on the model output

Why Sensitivity analysis?

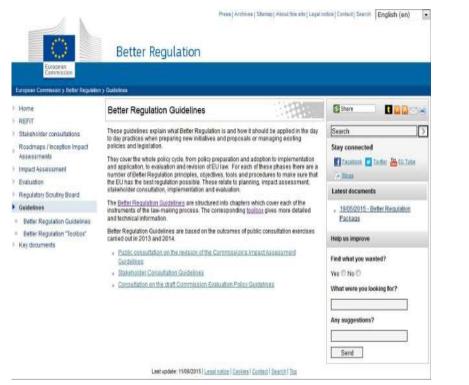
European Commission, 2015 Office for the Management and Budget, 2006 Environmental Protection Agency, 2009

EPA, 2009, March. Guidance on the Development, Evaluation, and Application of Environmental Models. Technical Report EPA/100/K-09/003. Office of the Science Advisor, Council for Regulatory Environmental Modeling, http://nepis.epa.gov/Exe/ZyPDF.cgi?Dockey=P1003E4R.PDF, Last accessed December 2015.

EUROPEAN COMMISSION, Better regulation toolbox, appendix to the Better Regulation Guidelines, Strasbourg, 19.5.2015, SWD(2015) 111 final, COM(2015) 215 final, http://ec.europa.eu/smart-regulation/guidelines/docs/swd_br_guidelines_en.pdf.

OMB, Proposed risk assessment bulletin, Technical report, The Office of Management and Budget's – Office of Information and Regulatory Affairs (OIRA), January 2006, https://www.whitehouse.gov/sites/default/files/omb/assets/omb/inforeg/proposed_risk_assessment_bulleti n_010906.pdf, pp. 16–17, accessed December 2015.

http://ec.europa.eu/smart-regulation/



Source: IA Toolbox, p. 391



EUROPEAN COMMISSION

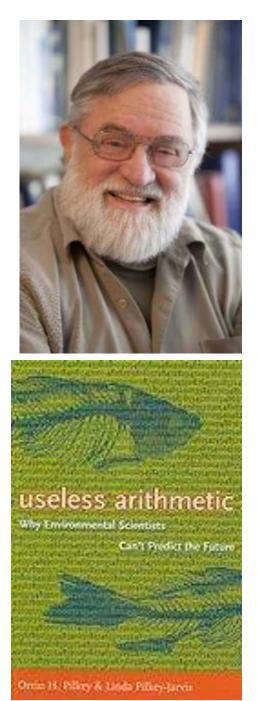


4. SENSITIVITY AND UNCERTAINTY ANALYSES Page 391

Six steps for a global SA:

- 1. Select <u>one</u> output of interest;
- 2. Participatory step: discuss which input may matter;
- 3. Participatory step (extended peer review): define distributions;
- 4. Sample from the distributions;
- 5. Run (=evaluate) the model for the sampled values;
- 6. Obtain in this way bot the uncertainty of the prediction and the relative importance of variables.

Limits of sensitivity analysis



Orrin H.

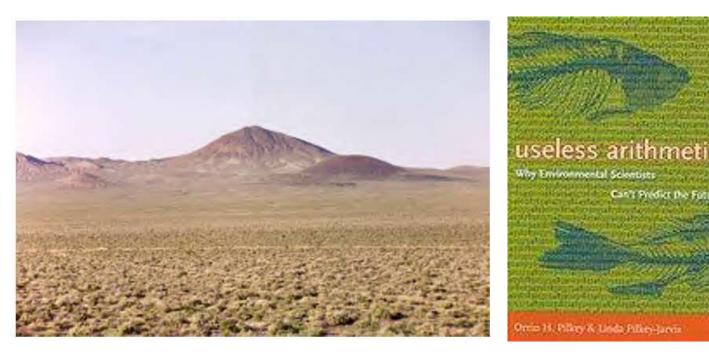
Pilkey

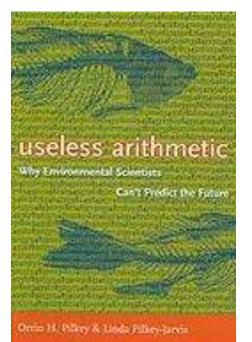
Useless Arithmetic: Why Environmental Scientists Can't Predict the Future by Orrin H. Pilkey and Linda Pilkey-Jarvis Useless arithmetic Wy Twine world Sciences Carl Productive Focus Orme 11, Pillery & Lable Pillery-Javes <>It is important, however, to recognize that the sensitivity of the parameter in the equation is what is being determined, not the sensitivity of the parameter in nature.

[…] If the model is wrong or if it is a poor representation of reality, determining the sensitivity of an individual parameter in the model is a meaningless pursuit.>>

One of the examples discussed concerns the Yucca Mountain repository for radioactive waste. TSPA model (for total system performance assessment) for safety analysis.

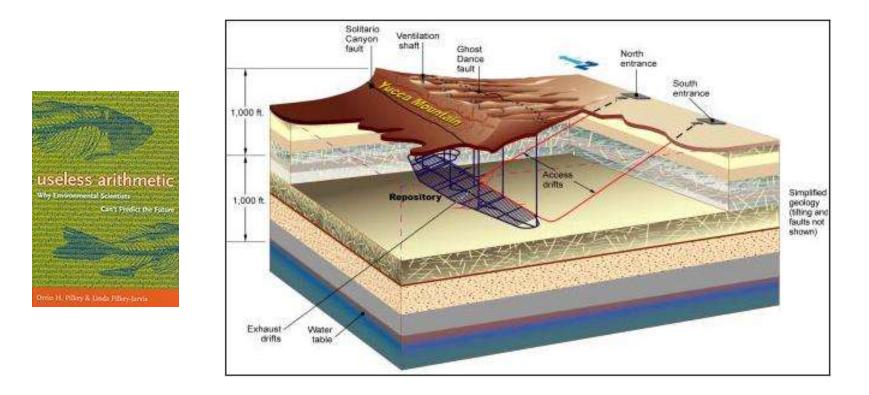
TSPA is Composed of 286 sub-models.





TSPA (like any other model) relies on assumptions \rightarrow one is the low permeability of the geological formation \rightarrow long time for the water to percolate from surface to disposal.

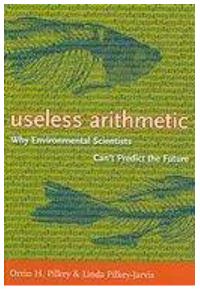




The confidence of the stakeholders in TSPA was not helped when evidence was produced which could lead to an upward revision of 4 orders of magnitude of this parameter (the ³⁶Cl story) Type III error in sensitivity: Examples:

In the case of TSPA (Yucca mountain) a range of 0.02 to 1 millimetre per year was used for percolation of flux rate.

→… SA useless if it is instead ~ 3,000 millimetres per year.





Robert K. Merton

"Scientific mathematical modelling should involve constant efforts to falsify the model"

Ref. → Robert K. Merton's 'Organized skepticism '

Communalism – the common ownership of scientific discoveries, according to which scientists give up intellectual property rights in exchange for recognition and esteem (Merton actually used the term Communism, but had this notion of communalism in mind, not Marxism);

Universalism – according to which claims to truth are evaluated in terms of universal or impersonal criteria, and not on the basis of race, class, gender, religion, or nationality;

Disinterestedness – according to which scientists are rewarded for acting in ways that outwardly appear to be selfless;

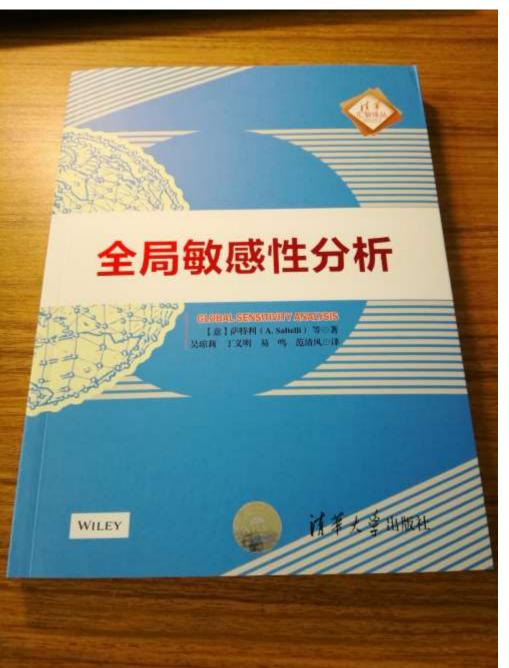
Organized Skepticism – all ideas must be tested and are subject to rigorous, structured community scrutiny.

A. Saltelli, M. Ratto, T. Andres, F. Campolongo, J. Cariboni, D. Gatelli, M. Saisana, S. Tarantola

GLOBAL SENSITIVITY ANALYSIS

The Primer

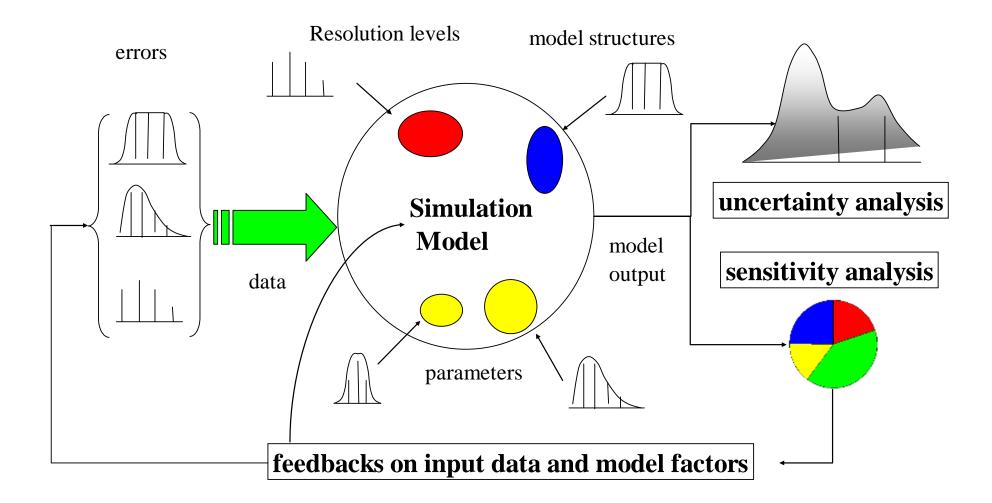
WILEY





Wu Qiongli

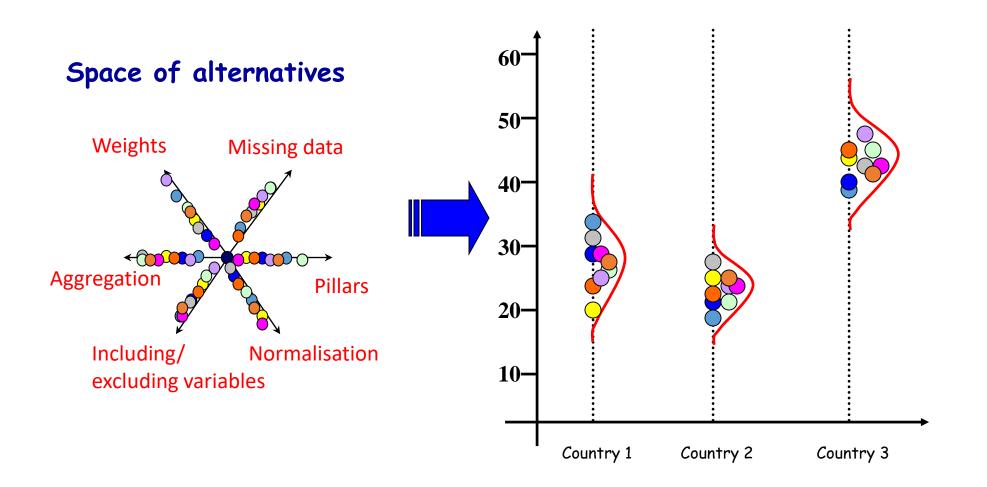
An engineer's vision of UA, SA



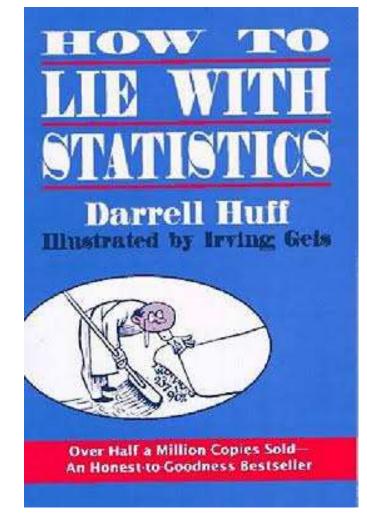
One can sample more than just factors

One can sample modelling assumptions, alternative data sets, resolution levels, scenarios …

| Assumption | Alternatives |
|----------------------|---|
| Number of indicators | all six indicators included or |
| | one-at-time excluded (6 options) |
| Weighting method | original set of weights, |
| | factor analysis, |
| | equal weighting, |
| | data envelopment analysis |
| Aggregation rule | additive, |
| | multiplicative, |
| | Borda multi-criterion |
| | |

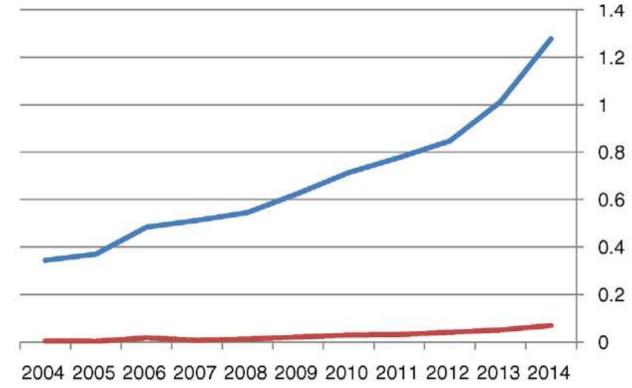


Can one lie with sensitivity analysis as one can lie with statistics?



Saltelli, A., Annoni P., 2010, How to avoid a perfunctory sensitivity analysis, Environmental Modeling and Software, 25, 1508–1517.

In 2014 out of 1000 papers in modelling 12 have a sensitivity analysis and < 1 a global SA; most SA still move one factor at a time

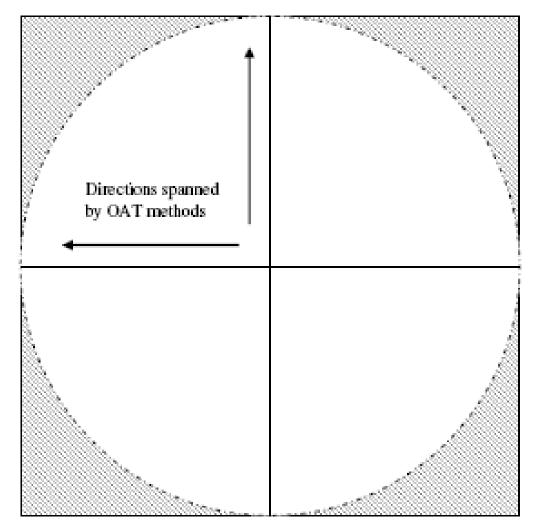


TOT SA/TOT MOD (%)

TOT GSA/TOT MOD (%)

Ferretti, F., Saltelli A., Tarantola, S., 2016, Trends in Sensitivity Analysis practice in the last decade, Science of the Total Environment, http://dx.doi.org/10.1016/j.scitotenv.201 6.02.133

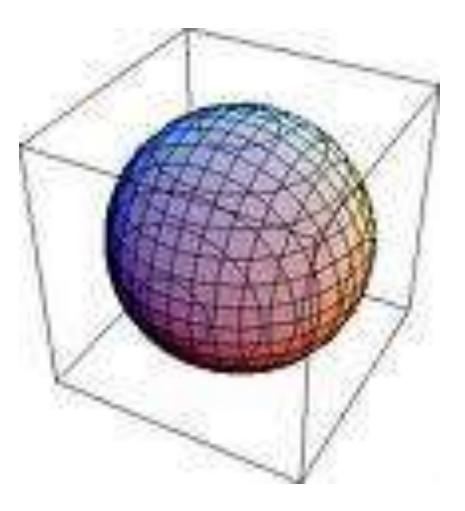
OAT in 2 dimensions



Area circle / area square =?

~ 3/4

OAT in 3 dimensions

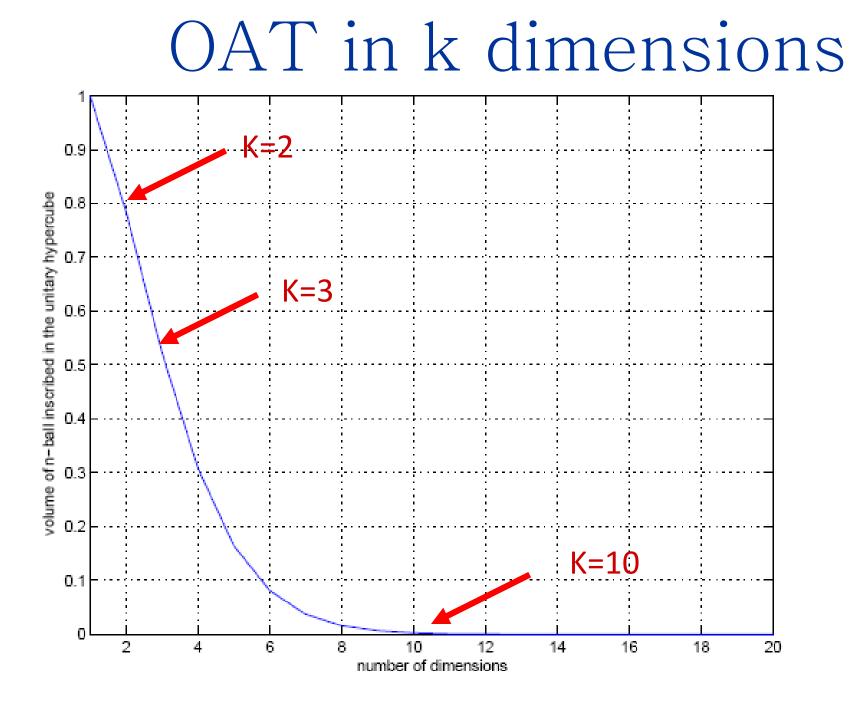


Volume sphere / volume cube =?

~ 1/2

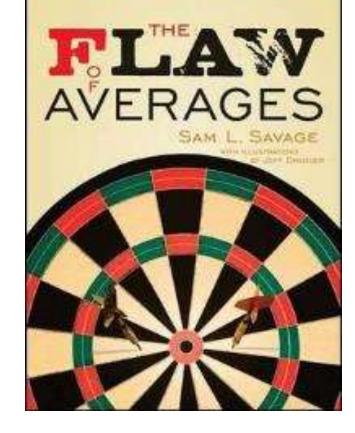
OAT in 10 dimensions; Volume hypersphere / volume ten dimensional hypercube =? ~ 0.0025





How would you test the scaffolding?

How coupled ladders are shaken in most of available literature How to shake coupled ladders



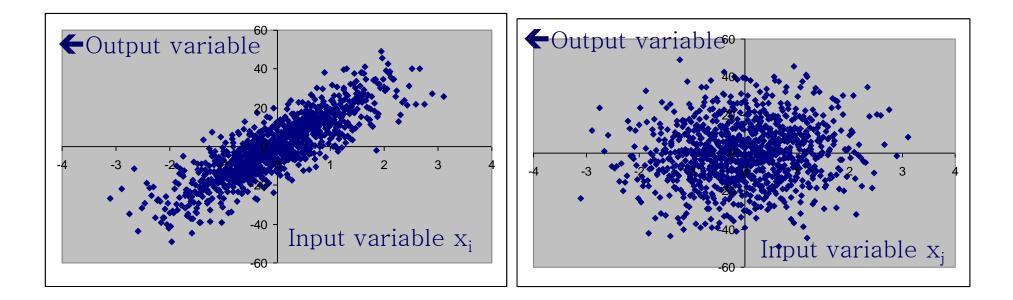
WHY WE UNDERESTIMATE RISK IN

THE FACE OF UNCERTAINTY

Once a sensitivity analysis is done via OAT there is no guarantee that either uncertainty analysis (UA) or sensitivity analysis (SA) will be any good:

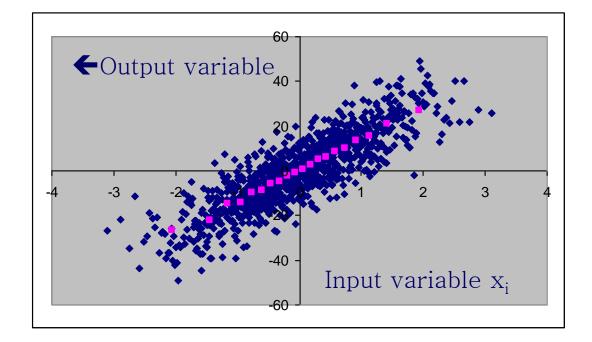
→ UA will be non conservative

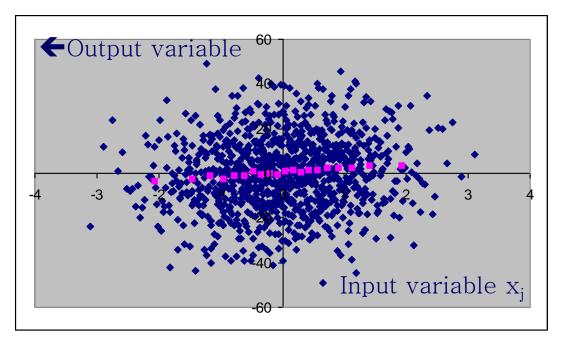
SA may miss important factors



Which factor is more important?

Why?

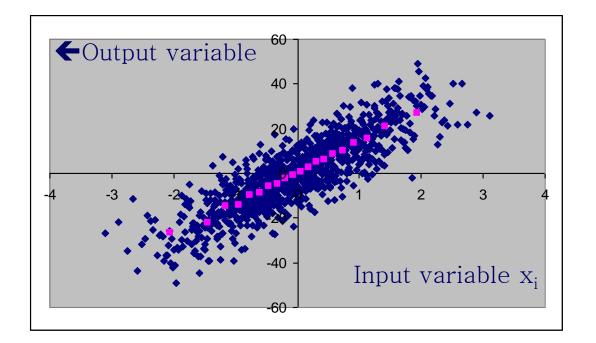




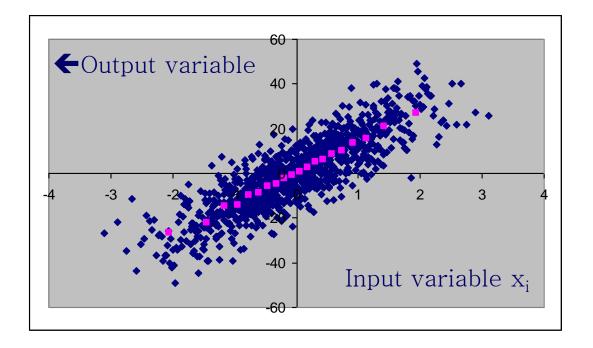
~1,000 blue points

Divide them in 20 bins of ~ 50 points

Compute the bin's average (pink dots)

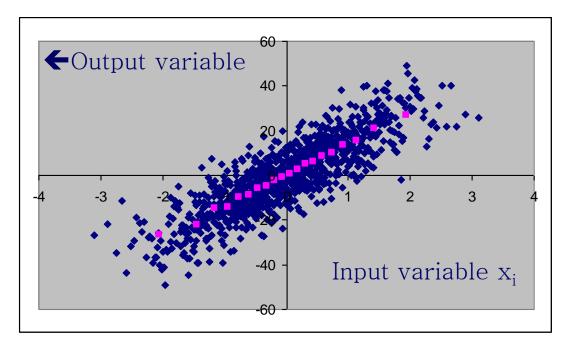


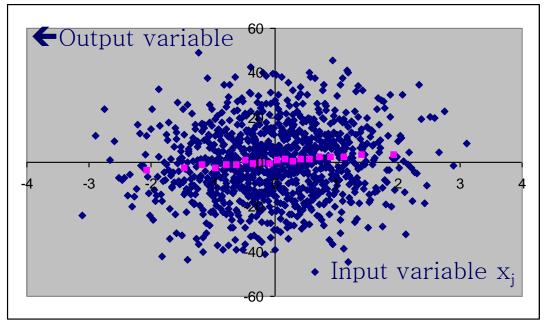
Each pink point is ~
$$E_{\mathbf{X}_{i}}(Y|X_{i})$$



Take the variance of the pink points and you have a sensitivity measure

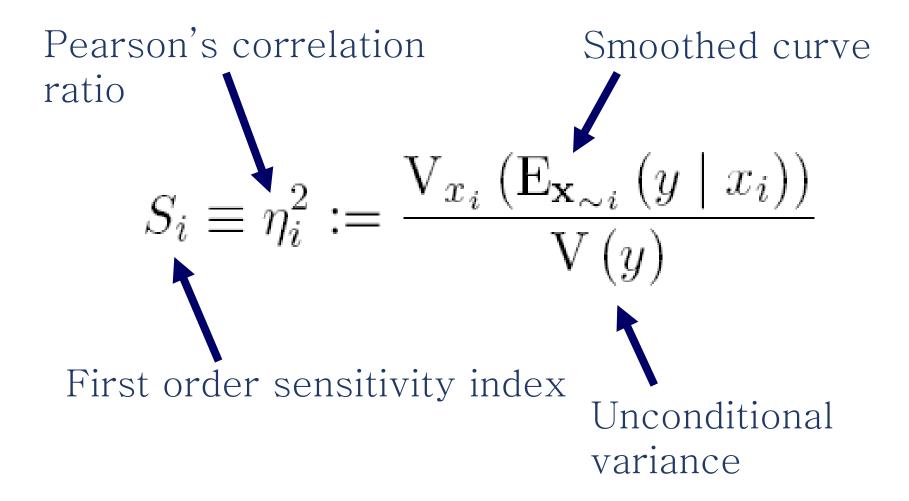
 $V_{X_i}\left(E_{\mathbf{X}_{\mathbf{x}_i}}\left(Y|X_i\right)\right)$

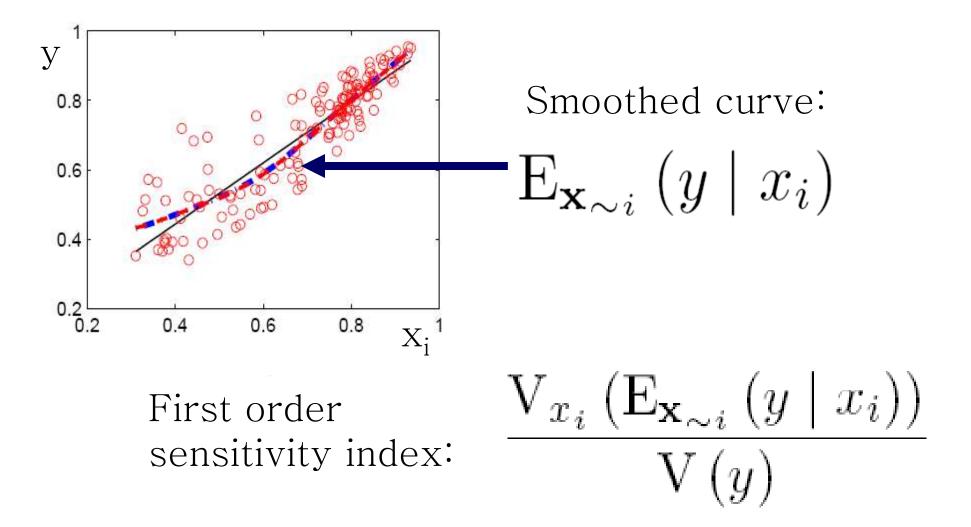




Which factor has the highest $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right)$?

 $S_i \equiv \frac{V(E(Y|X_i))}{V_Y}$





 $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right)$

- First order effect, or top marginal variance=
- = the expected reduction in variance that would be achieved if factor Xi could be fixed.
- Why?

Because:

 $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right) +$ $+ E_{X_i}\left(V_{\mathbf{X}_i}\left(Y | X_i\right)\right) = V(Y)$

Easy to prove using $V(Y)=E(Y^2)-E^2(Y)$

Because:

 $V_{\underline{X}_{i}}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_{i}\right)\right)+$ $+ E_{X_i} \left(V_{\mathbf{X}_{\sim i}} \left(Y | X_i \right) \right) = V(Y)$

This is what variance would be left (on average) if Xi could be fixed…

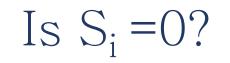
must be the expected reductionin variance that would be achievedif factor Xi could be fixed

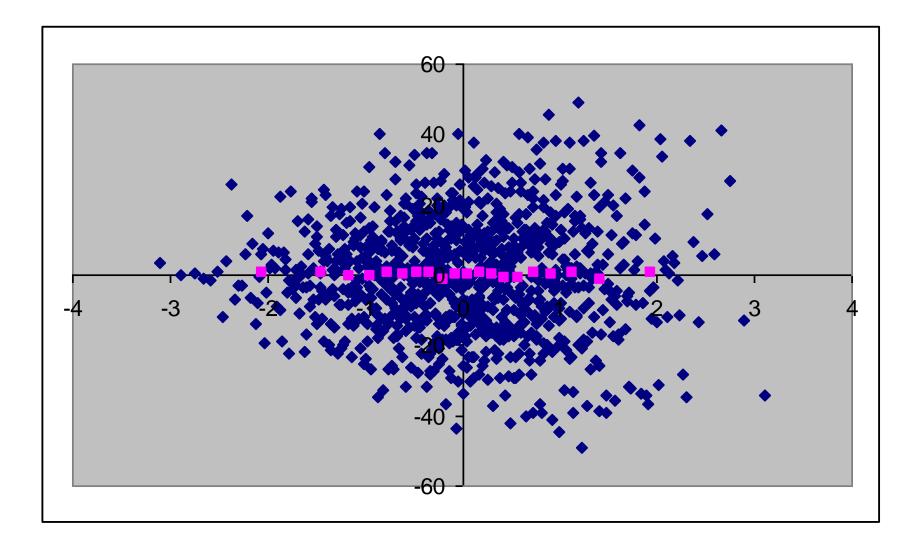
For <u>additive</u> models one can decompose the total variance as a sum of first order effects

 $\sum V_{X_i} \left(E_{\mathbf{X}_{\sim i}} \left(Y | X_i \right) \right) \approx V(Y)$

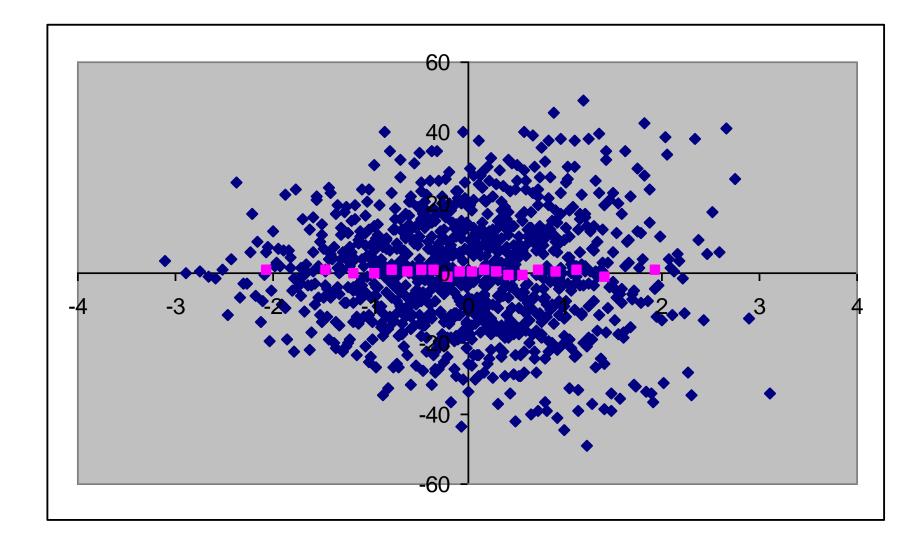
··· which is also how additive models are defined

Non additive models





Is this factor non-important?



There are terms which capture two-way, three way, … interactions among variables.

All these terms are linked by a formula

Variance decomposition (ANOVA)

V(Y) =

$\sum_{i} V_{i} + \sum_{i,j>i} V_{ij} + \dots + V_{123\dots k}$

→ Lesson Stefano Tarantola

EC impact assessment guidelines: sensitivity analysis & auditing

| Conversion | in) Gudelinea | |
|--|---|---|
| Home | Better Regulation Guidelines | 💽 Share 🚺 🛄 |
| REFIT Stakeholder consultations Roadmaps / Inception Impact | These guidelines explain what Better Regulation is and how it should be applied in the day to day practices when preparing new initiatives and proposals or managing existing policies and legislation. | Search |
| | | Stay connected |
| Assessments | They cover the whole policy cycle, from policy preparation and adoption to implementation | Tricebook 💟 Twitter 🚜 0 |
| Impact Assessment | and application, to evaluation and revision of EU law. For each of these phases there a number of Better Regulation principles, objectives, tools and procedures to make sure | a true |
| Evaluation | the EU has the best regulation possible. These relate to planning, impact assessment, stakeholder consultation, implementation and evaluation. | Latest documents |
| Regulatory Scrutiny Board | The Better Regulation Guidelines are structured into chapters which cover each of the | |
| Guidelines Batter Resultation Cuidelines | instruments of the law-mailing process. The corresponding tooloor gives more detailed and technical information | <u>19/05/2015 - Better Regul</u> Package |
| Better Regulation Guidelines Better Regulation "Toolbox" Key documents | Better Regulation Guidelines are based on the outcomes of public consultation exercises carried out in 2013 and 2014. | Help us improve |
| (top) water raine | Public consultation on the revision of the Commission's Impact Assessment Guidelines | Find what you wanted? |
| | Stakeholder Consultation Goldelines | YHS C No C |
| | Genauftation on the draft Commission Evaluation Policy Guidelines | What were you looking for? |
| | | Any suggestions? |

http://ec.europa.eu/smart-regulation/guidelines/docs/br_toolbox_en.pdf

Secrets of sensitivity analysis

Why should one ever run a model just once? First secret: The most important question is the question.

Or: sensitivity analysis is not "run" on a model but on a model once applied to a question Second secret: Sensitivity analysis should not be used to hide assumptions [it often is]



Third secret: If sensitivity analysis shows that a question cannot be answered by the model one should find another question or model

[Often the love for one's own model prevails]

Badly kept secret:

There is always one more bug!

(Lubarsky's Law of Cybernetic Entomology)



And of course please don't run a sensitivity analysis where each factors has a 5% uncertainty



More than a technical uncertainty and sensitivity analysis? 1. Uncertainty and sensitivity analysis (never execute the model once)

2. Sensitivity auditing and quantitative storytelling (investigate frames and motivations)

Saltelli, A., Guimarães Pereira, Â., Van der Sluijs, J.P. and Funtowicz, S., 2013, 'What do I make of your latinorum? Sensitivity auditing of mathematical modelling', Int. J. Foresight and Innovation Policy, (9), 2/3/4, 213–234.

Saltelli, A., Does Modelling need a reformation? Ideas for a new grammar of modelling, available at https://arxiv.org/abs/1712.06457

3. Replace 'model to predict and control the future' with 'model to help mapping ignorance about the future' ...

... in the process exploiting and making explicit the metaphors embedded in the model

J. R. Ravetz, "Models as metaphors," in Public participation in sustainability science : a handbook, and W. A. B. Kasemir, J. Jäger, C. Jaeger, Gardner Matthew T., Clark William C., Ed. Cambridge University Press, 2003, available at http://www.nusap.net/download.php?op=getit&lid=11

END

