

Sensitivity analysis, an introduction

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Where to find this talk: www.andreasaltelli.eu



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29/07/2019

On sensitivity analysis and its take up

Definitions

Uncertainty analysis: Focuses on quantifying the uncertainty in model output

Sensitivity analysis: The study of the relative importance of different input factors on the model output

A. Saltelli, M. Ratto, T. Andres, F. Campolongo, J. Cariboni, D. Gatelli, M. Saisana, S. Tarantola

GLOBAL SENSITIVITY ANALYSIS The Primer

WILEY





Dr. Qiongli Wu, Wuhan Institute of Physics and Mathematics, Chinese Academy of Sciences, Wuhan, China

European Commission, 2015 Office for the Management and Budget, 2006 Environmental Protection Agency, 2009

EPA, 2009, March. Guidance on the Development, Evaluation, and Application of Environmental Models. Technical Report EPA/100/K-09/003. Office of the Science Advisor, Council for Regulatory Environmental Modeling, http://nepis.epa.gov/Exe/ZyPDF.cgi?Dockey=P1003E4R.PDF, Last accessed December 2015.

EUROPEAN COMMISSION, Better regulation toolbox, appendix to the Better Regulation Guidelines, Strasbourg, 19.5.2015, SWD(2015) 111 final, COM(2015) 215 final, http://ec.europa.eu/smart-regulation/guidelines/docs/swd_br_guidelines_en.pdf.

OMB, Proposed risk assessment bulletin, Technical report, The Office of Management and Budget's – Office of Information and Regulatory Affairs (OIRA), January 2006, https://www.whitehouse.gov/sites/default/files/omb/assets/omb/inforeg/proposed_risk_assessment_bulleti n_010906.pdf, pp. 16–17, accessed December 2015.



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Better Regulation

European Commission > Better Regulation > Guidelines

- Home
- REFIT
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- Impact Assessment
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- Regulatory Scrutiny Board
- Guidelines
- Better Regulation Guidelines
- Better Regulation "Toolbox"
- Key documents

Better Regulation Guidelines

These guidelines explain what Better Regulation is and how it should be applied in the day to day practices when preparing new initiatives and proposals or managing existing policies and legislation.

They cover the whole policy cycle, from policy preparation and adoption to implementation and application, to evaluation and revision of EU law. For each of these phases there are a number of Better Regulation principles, objectives, tools and procedures to make sure that the EU has the best regulation possible. These relate to planning, impact assessment, stakeholder consultation, implementation and evaluation.

The <u>Better Regulation Guidelines</u> are structured into chapters which cover each of the instruments of the law-making process. The corresponding <u>toolbox</u> gives more detailed and technical information.

Better Regulation Guidelines are based on the outcomes of public consultation exercises carried out in 2013 and 2014.

- Public consultation on the revision of the Commission's Impact Assessment Guidelines
- Stakeholder Consuitation Guidelines
- Consultation on the draft Commission Evaluation Policy Guidelines



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http://ec.europa. eu/smartregulation/ Source: IA Toolbox, p. 391

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An engineer's vision of UA, SA



One can sample more than just factors:

- modelling assumptions,
- alternative data sets,
- resolution levels,
- scenarios …

Assumption	Alternatives
Number of indicators	all six indicators included or
	one-at-time excluded (6 options)
Weighting method	 original set of weights,
	 factor analysis,
	 equal weighting,
	 data envelopment analysis
Aggregation rule	 additive,
	 multiplicative,
	 Borda multi-criterion



Why sensitivity analysis

IDENCE. ARGUMENT.& **RSUASION IN** -IF POLICY **CESS**

"Are the results from a particular model more sensitive to changes in the model and the methods used to estimate its parameters, or to changes in the data?" Why sensitivity analysis

··· SA can tell



Model Complexity

Presented as 'Conjecture by O'Neill'

In M. G. Turner and R. H. Gardner, "Introduction to Models" in Landscape Ecology in Theory and Practice, New York, NY: Springer New York, 2015, pp. 63–95.

Why sensitivity analysis

Also known as Zadeh's principle of incompatibility, whereby as complexity increases "precision and significance (or relevance) become almost mutually exclusive characteristics"

L. Zadeh, "Outline of a New Approach to the Analysis of Complex Systems and Decision Processes," IEEE Trans. Syst. Man. Cybern., vol. 3, no. 1, pp. 28-44, 1973.



Model complexity

Model-based knowing is conditional; SA explains this conditionality Why sensitivity analysis SA can detect garbage in garbage out (GIGO)

Why sensitivity analysis

Funtowicz & Ravetz's GIGO (Garbage In, Garbage Out) Science "where uncertainties in inputs must be suppressed least outputs become indeterminate"

Leamer's "Conclusions are judged to be sturdy only if the neighborhood of assumptions is wide enough to be credible and the corresponding interval of inferences is narrow enough to be useful"

S. Funtowicz and J. R. Ravetz, *Uncertainty and Quality in Science for Policy*. Dordrecht: Kluwer, 1990; E. E. Leamer, "Sensitivity Analyses Would Help," *Am. Econ. Rev.*, vol. 75, no. 3, pp. 308–313, 1985. Global Environmental Change 20 (2010) 298-302



Sensitivity analysis didn't help. A practitioner's critique of the Stern review Andrea Saltelli*, Beatrice D'Hombres

Joint Research Centre, Institute for the Protection and Security of the Citizen, Ispra, Italy

The case of Stern's Review – Technical Annex to postscript



Nicholas Stern, London School of Economics

Stern, N., Stern Review on the Economics of Climate Change. UK Government Economic Service, London, <u>www.sternreview.org.uk</u>.

William Nordhaus, University of Yale Nobel 'Economics' 2018

Nordhaus W., Critical Assumptions in the Stern Review on Climate Change, SCIENCE, 317, 201–202, (2007).

How was it done? A reverse engineering of the analysis

Missing points



% loss in GDP per capita



Climate Models as Economic Guides: Scientific Challenge or Quixotic Quest?

BY ANDREA SALTELLI, PHILIP B. STARK, WILLIAM BECKER, PAWEL STANO

Finding all sorts of surprises



Journal of the Royal Statistical Society





J. R. Statist. Soc. A (2013) **176**, *Part* 3, *pp*. 609–634

Ratings and rankings: voodoo or science?

Paolo Paruolo

University of Insubria, Varese, Italy

and Michaela Saisana and Andrea Saltelli European Commission, Ispra, Italy





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Exploring Hoover and Perez's experimental designs using global sensitivity analysis

William Becker, Paolo Paruolo, Andrea Saltelli

(Submitted on 22 Jan 2014)

This paper investigates variable-selection procedures in regression that make use of global sensitivity analysis. The approach is combined with existing algorithms and it is applied to the time series regression designs proposed by Hoover and Perez. A comparison of an algorithm employing global sensitivity analysis and the (optimized) algorithm of Hoover and Perez shows that the former significantly improves the recovery rates of original specifications.

Why sensitivity analysis

Why using variance-based sensitivity analysis methods



Plotting the output as a function of two different input factors

Which factor is more important?





~1,000 blue points

Divide them in 20 bins of ~ 50 points

Compute the bin's average (pink dots)



Each pink point is ~
$$E_{\mathbf{X}_{\sim i}}(Y|X_i)$$



Take the variance of the pink points one obtains a sensitivity measure

 $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right)$





Which factor has the highest $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right)$?

 $S_i \equiv \frac{V(E(Y|X_i))}{V_Y}$





 $V_{X_i}\left(E_{\mathbf{X}_i}\left(Y|X_i\right)\right)$

First order effect, or top marginal variance = the expected reduction in variance that would be achieved if factor Xi could be fixed.

Why?
Because:

 $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right) +$ $+ E_{X_i}\left(V_{\mathbf{X}_{\mathbf{x}_i}}\left(Y | X_i\right)\right) = V(Y)$

Easy to prove using $V(Y)=E(Y^2)-E^2(Y)$



Because:

 $V_{X_i}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right) +$ $+ E_{X_i}\left(V_{\mathbf{X}_{\sim i}}\left(Y|X_i\right)\right) = V(Y)$

This is the variance when a factor Xi is fixed …

Because:

 $V_{\underline{X}_{i}}\left(E_{\mathbf{X}_{\sim i}}\left(Y|X_{i}\right)\right)+$ $+ E_{X_i} \left(V_{\mathbf{X}_{\sim i}} \left(Y | X_i \right) \right) = V(Y)$

This is what variance would be left (on average) if Xi could be fixed…

must be the expected reductionin variance that would be achievedif factor Xi could be fixed

For <u>additive</u> models one can decompose the total variance as a sum of first order effects

 $\sum V_{X_i} \left(E_{\mathbf{X}_{\sim i}} \left(Y | X_i \right) \right) \approx V(Y)$

··· which is also how additive models are defined

Non additive models can also be effectively dealt with, in the context of variance decomposition theory

Possibility to compute effectively total sensitivity indices

Summary: advantages with variance based methods:

- graphic interpretation scatterplots
- statistical interpretation
- expressed plain English
- (working with sets)
- (relation to settings)



Limit of SA: The map is not the territory



Orrin H.

Pilkey



Useless Arithmetic: Why Environmental Scientists Can't Predict the Future by Orrin H. Pilkey and Linda Pilkey-Jarvis, Columbia University Press, 2009.

Onio H. Piley & Linda Pilicy-Jawa

Useless arithmetic Wy Informetial Sciences Cara Predict the Fictor Other 11, Pilkey & Lieda Pilkey-Juwa <>It is important to recognize that the sensitivity of the parameter in the equation is what is being determined, not the sensitivity of the parameter in nature.

[…] If the model is wrong or if it is a poor representation of reality, determining the sensitivity of an individual parameter in the model is a meaningless pursuit.>>

One of the examples discussed concerns the Yucca Mountain repository for radioactive waste. TSPA model (for total system performance assessment) for safety analysis.

TSPA is Composed of 286 sub-models.





TSPA (like any other model) relies on assumptions \rightarrow one is the low permeability of the geological formation \rightarrow long time for the water to percolate from surface to disposal.





Evidence was produced leading to an upward revision of 4 orders of magnitude of this parameter (the ³⁶Cl story) In the model a range of 0.02 to 1 millimetre per year was used for percolation of flux rate.

→… SA useless if it is instead ~ 3,000 millimetres per year.





"Scientific mathematical modelling should involve constant efforts to falsify the model"

Ref. → Robert K. Merton's 'Organized skepticism '

Communalism – the common ownership of scientific discoveries, according to which scientists give up intellectual property rights in exchange for recognition and esteem (Merton actually used the term Communism, but had this notion of communalism in mind, not Marxism);

Universalism – according to which claims to truth are evaluated in terms of universal or impersonal criteria, and not on the basis of race, class, gender, religion, or nationality;

Disinterestedness – according to which scientists are rewarded for acting in ways that outwardly appear to be selfless;

Robert K. Merton Organized Skepticism - all ideas must be tested and are subject to rigorous, structured community scrutiny.

Limit of SA: Often no SA or wrong kind of SA applied Science of the Total Environment 568 (2016) 666-670



Contents lists available at ScienceDirect

Science of the Total Environment

journal homepage: www.elsevier.com/locate/scitotenv

Trends in sensitivity analysis practice in the last decade

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^d Institut de Ciència i Tecnologia Ambientals (ICTA), Universitat Autonoma de Barcelona, Spain



Total Environmen

In 2014 out of 1000 papers in modelling 12 have a sensitivity analysis and < 1 a global SA; most SA still move one factor at a time



____ TOT_SA/TOT_MOD (%)
____ TOT_GSA/TOT_MOD (%)

Environmental Modelling & Software 25 (2010) 1508-1517



How to avoid a perfunctory sensitivity analysis

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OAT in 2 dimensions



Area circle / area square =?

~ 3/4

OAT in 3 dimensions



Volume sphere / volume cube =?

~ 1/2

OAT in 10 dimensions; Volume hypersphere / volume ten dimensional hypercube =? ~ 0.0025







Environmental Modelling & Software

Volume 114, April 2019, Pages 29-39



Why so many published sensitivity analyses are false: A systematic review of sensitivity analysis practices

Andrea Saltelli ^{a, b} 은 쩓, Ksenia Aleksankina ^c, William Becker ^d, Pamela Fennell ^e, Federico Ferretti ^d, Niels Holst ^f, Sushan Li ^g, Qiongli Wu ^h

A systematic review of 280 scientific papers mentioning sensitivity analysis, focusing on highly cited works

42% of highly cited papers present a SA of poor quality

Beyond sensitivity analysis: sensitivity auditing

SAPEA report 2019



SATPEA

Science Advice for Policy by European Academies



VOL. XXX, NO. 2, WINTER 2014

When All Models Are Wrong

BY ANDREA SALTELLI, SILVIO FUNTOWICZ

The rules of sensitivity auditing

- 1. Check against rhetorical use of mathematical modelling;
- 2. Adopt an "assumption hunting" attitude; focus on unearthing possibly implicit assumptions;
- 3. Check if uncertainty been instrumentally inflated or deflated.

4. Find sensitive assumptions before these find you; do your SA before publishing;

5. Aim for transparency; Show all the data;

- 6. Do the right sums, not just the sums right;
- 7. Perform a proper global sensitivity analysis.

On modelling



Comment Open Access Published: 27 August 2019

A short comment on statistical versus mathematical modelling



The Economist

OCTOBER 10TH-25TH 2013

Economist.com

Washington's lawyer surplus How to do a nuclear deal with Iran Investment tips from Nobel economists Junk bonds are back The meaning of Sachin Tendulkar



On the radar: October 2013



Futures Volume 91, August 2017, Pages 5-11



What is science's crisis really about?

Andrea Saltelli ^{a, b} 유 핵, Silvio Funtowicz ^a





Why science's crisis should not become a political battling ground

Andrea, Saltelli 🖾



Crisis in statistics?





As debate rumbles on about how and how much poor statistics is to blame for poor reproducibility, Nature asked influential statisticians to recommend one change to improve science. The common theme? The problem is not our maths, but ourselves.
CORRESPONDENCE · 16 JANUARY 2018



Fixing statistics is more than a technical issue

Andrea Saltelli & Philip Stark

https://www.nature.com/articles/d41586-018-00647-9

CORRESPONDENCE · 16 JANUARY 2018



Integrity must underpin quality of statistics



https://www.nature.com/articles/d41586-018-00648-8

All users of statistical techniques, as well as those in other mathematical fields such as modelling and algorithms, need an effective societal commitment to the maintenance of quality and integrity in their work (Ravetz, 2018)

If imposed alone, technical or administrative solutions will only breed manipulation and evasion (Ravetz, 2018)





Throw away the concept of statistical significance?





COMMENT · 20 MARCH 2019

Scientists rise up against statistical significance

Valentin Amrhein, Sander Greenland, Blake McShane and more than 800 signatories call for an end to hyped claims and the dismissal of possibly crucial effects.

Valentin Amrhein 🖾, Sander Greenland & Blake McShane

See the discussion on the blog of Andrew Gelman https://statmodeling.stat.columbia.edu/

Is mathematical modelling affected?

Need for a more structured, generalized and standardized approach to verification

Padilla, J. J., Diallo, S. Y., Lynch, C. J., & Gore, R. (2018). Observations on the practice and profession of modeling and simulation: A survey approach. SIMULATION, 94(6), 493–506.

Unlike statistics, modelling is not a discipline …

··· mathematical modelling cannot do this:



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AMERICAN STATISTICAL ASSOCIATION RELEASES STATEMENT ON STATISTICAL SIGNIFICANCE AND P-VALUES

Provides Principles to Improve the Conduct and Interpretation of Quantitative Science March 7, 2016

Wasserstein, R.L. and Lazar, N.A., 2016. 'The ASA's statement on p-values: context, process, and purpose', The American Statistician, Volume 70, 2016 – Issue 2, Pages 129–133.

Algorithms, models, metrics, statistics



Common root causes?

Statistics could help by internalizing techniques for validation and verification (including sensitivity analysis) in its syllabi



Paula Rego, Self portrait in red (1962), detail, MNAC, Barcelona

CALL FOR PAPERS for the Ninth International Conference on Sensitivity Analysis of Model Output

Barcelona, October Monday 28 - Wednesday 30, 2019



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END



What is modelling?

Modelling as a craft rather than as a science for Robert Rosen



R. Rosen, Life Itself: A Comprehensive Inquiry Into the Nature, Origin, and Fabrication of Life. Columbia University Press, 1991.





Robert Rosen

"models are most useful when they are used to challenge existing formulations, rather than to validate or verify them"



Naomi Oreskes

N. Oreskes, K. Shrader-Frechette, and K. Belitz, "Verification, Validation, and Confirmation of Numerical Models in the Earth Sciences," Science, 263, no. 5147, 1994.

Models are not physical laws



Oreskes, N., 2000, Why predict? Historical perspectives on prediction in Earth Science, in Prediction, Science, Decision Making and the future of Nature, Sarewitz et al., Eds., Island Press, Washington DC "[…] to be of value in theory testing, the predictions involved must be capable of refuting the theory that generated them" (N. Oreskes)



"In many cases, these temporal predictions are treated with the same **respect** that the hypothetic-deductive model of science accords to logical predictions. But this respect is largely misplaced"



"[…] models are complex amalgam of theoretical and phenomenological laws (and the governing equations and algorithms that represent them), empirical input parameters, and a model conceptualization […] When a model generates a prediction, of what precisely is the prediction a test? The laws? The input data? The conceptualization? Any part (or several parts) of the model might be in error, and there is no simple way to determine which one it is"



Economics

Paul Romer's Mathiness = use of mathematics to veil normative stances

Erik Reinert: scholastic tendencies in the mathematization of economics

P. M. Romer, "Mathiness in the Theory of Economic Growth," Am. Econ. Rev., vol. 105, no. 5, pp. 89–93, May 2015.

E. S. Reinert, "Full circle: economics from scholasticism through innovation and back into mathematical scholasticism," J. Econ. Stud., vol. 27, no. 4/5, pp. 364–376, Aug. 2000.

Variance based methods for non additive models





Is this factor non-important?



Variance decomposition (ANOVA)

V(Y) =

 $\sum_{i} V_{i} + \sum_{i,j>i} V_{ij} + \dots + V_{123\dots k}$

Variance decomposition (ANOVA)

When the factors are independent the total variance can be decomposed into main effects and interaction effects up to the order k, the dimensionality of the problem.

Thus given a model $Y=f(X_1, X_2, X_3)$

Decomposition:

 $V = V_{1} + V_{2} + V_{3} + V_{12} + V_{12} + V_{13} + V_{23} + V_{12} + V_{123} + V_{23} + V_{123}$

Thus given a model $Y=f(X_1, X_2, X_3)$

- Same decomposition divided by V
- $1 = S_1 + S_2 + S_3 + S_{12} + S_{13} + S_{23} + S_{13} + S_{23} + S_{13} + S_{23} + S_{23}$
- $+S_{123}$

One may be interested in the total effects:

 $S_{T1} = S_1 + S_{12} + S_{13} + S_{123}$

(and analogue formulae for S_{T2} , S_{T3}) which can be computed without knowing S_1 , S_{12} , S_{13} , S_{123}

 $S_{T1} \mbox{ is called a total effect sensitivity index }$

$E_{\mathbf{X}_{\sim i}}\left(V_{X_{i}}\left(Y|\mathbf{X}_{\sim i}\right)\right)$

Total effect, or bottom marginal variance=

= the expected variance that would be left if all factors but Xi could be fixed (self evident definition) Total effect, or bottom marginal variance=

= the expected variance that would be left if all factors but Xi could be fixed (self evident definition)

 $S_{Ti} \equiv \frac{E(V(Y|\mathbf{X}_{\sim i}))}{V_Y}$