

Sensitivity analysis

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Where to find this talk: www.andreasaltelli.eu

The image shows a screenshot of the website www.andreasaltelli.eu. The browser address bar at the top displays the URL. The website header features a teal square with the name "Andrea Saltelli" in white. Below this is a navigation menu with the following items: HOME, ABOUT ME, PUBLICATIONS, NEWS & VIDEOS, and RESOURCES. A red arrow points from the search bar area down to the "RESOURCES" menu item. A dropdown menu is open under "RESOURCES", showing "PRESENTATIONS" and "OTHER RESOURCES". The main content area has a background image of terraced rice fields with the text "CAETERIS ARE NEVER PARIBUS" overlaid. A tweet overlay is visible on the right side, featuring a profile picture of Andrea Saltelli, his name "@AndreaSaltelli", and the text: "Thoughts on Ioannidis' latest article: onlinelibrary.wiley.com/doi/10.1111/ec... theconversation.com/sciences-credi... via @TC_Africa". The tweet includes an image of a microscope and a snippet of text: "Science's credibility crisis: why it will g... We are observing two new phenomena... theconversation.com".

Blurring lines:

“what qualities are specific to rankings, or indicators, or models, or algorithms?”

E. Popp Berman and D. Hirschman, *The Sociology of*

Quantification: Where Are We Now?, *Contemp. Sociol.*, vol. in press, 2017.

“[in climate modelling] it looks very little like our idealized image of science, in which pure theory is tested with pure data.

[impossible to] eliminate the model-dependency of data or the data-ladenness of models”

Paul N. Edwards, 1999, Global climate science, uncertainty and politics:
Data-laden models, model-filtered data.

“[For] philosophers Frederick Suppe and Stephen Norton the blurry model/data relationship pervades all science”

Paul N. Edwards, 1999, Global climate science, uncertainty and politics:

Data-laden models, model-filtered data.

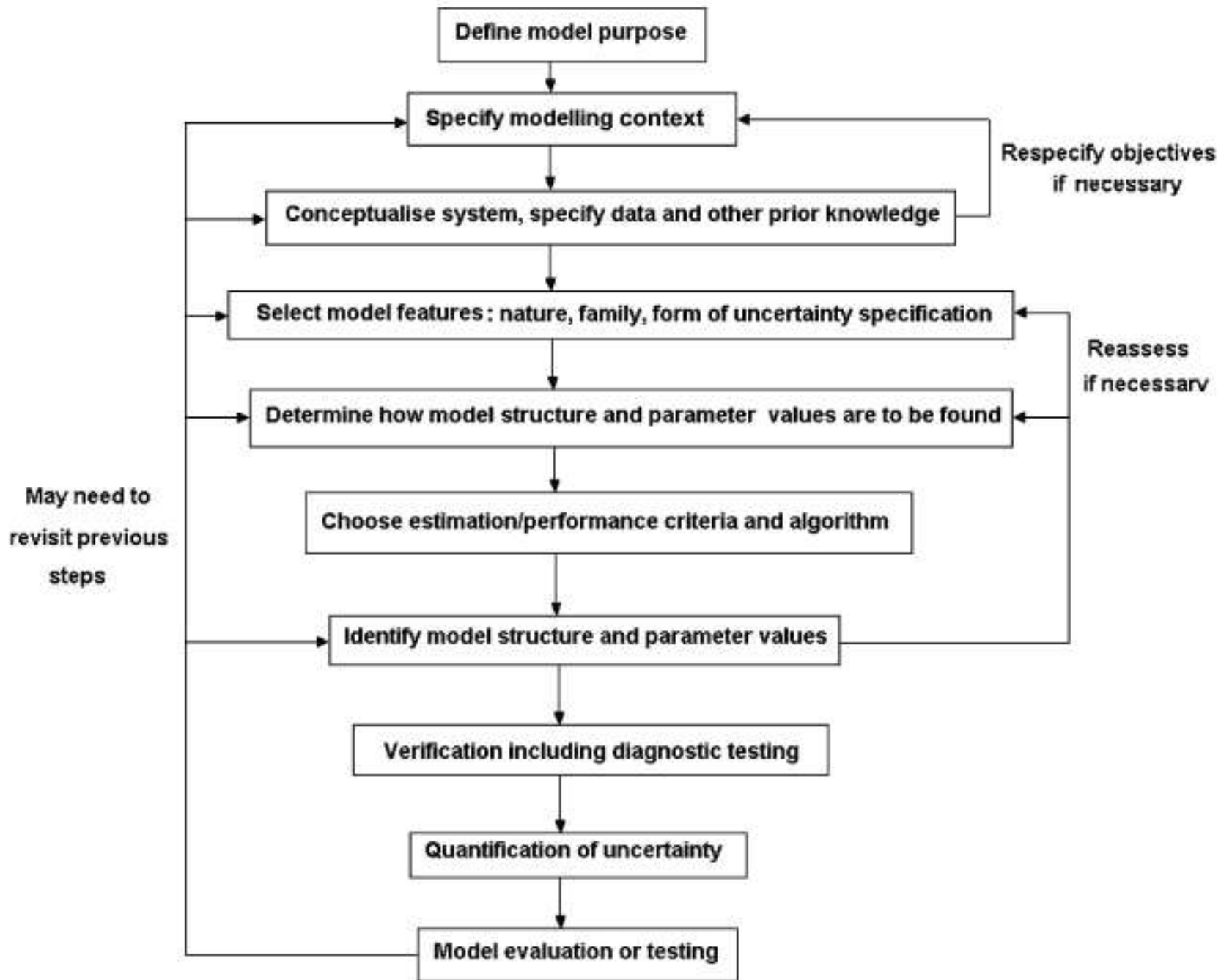
Padilla et al. call for a more structured, generalized and standardized approach to verification

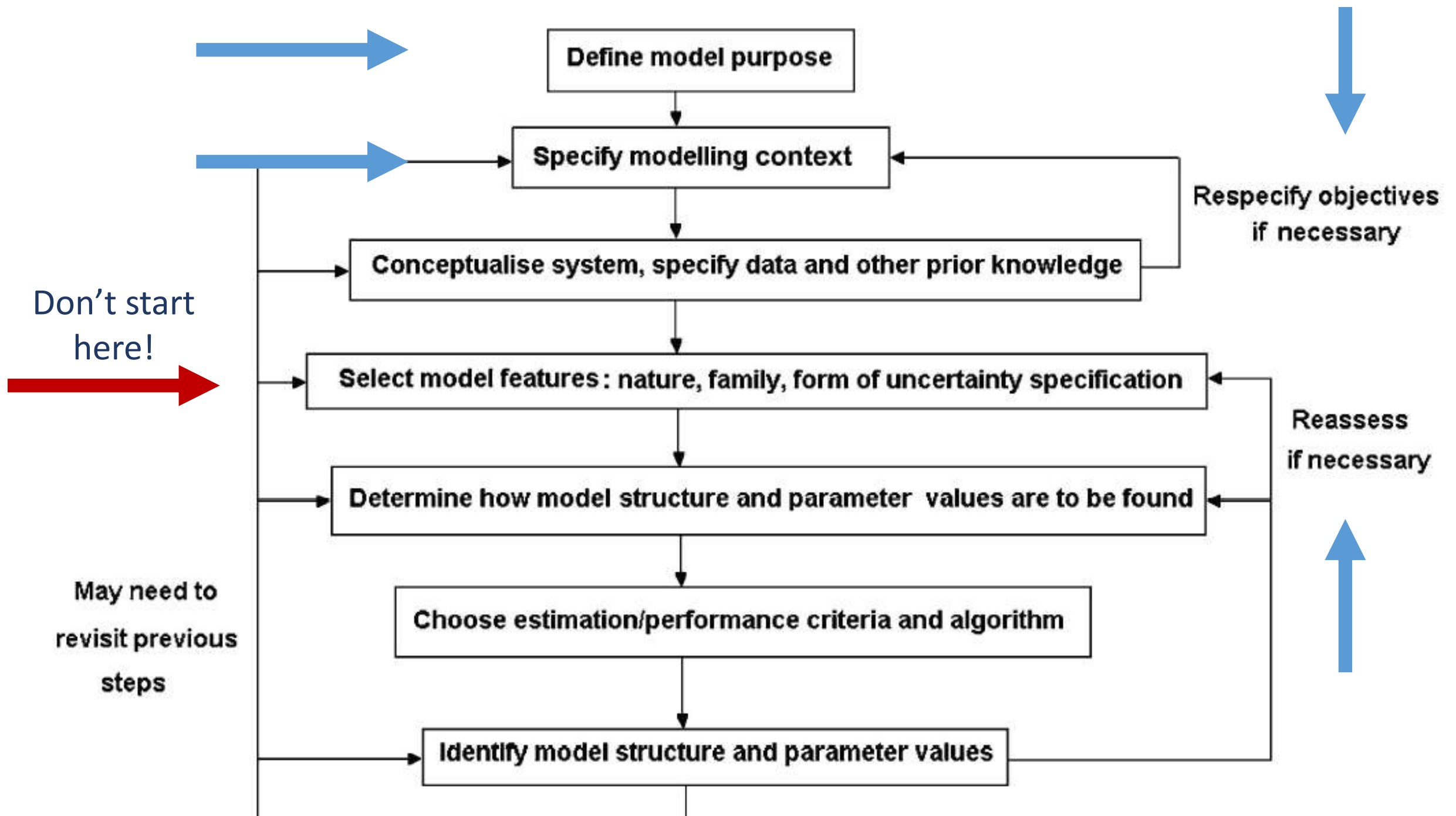
Jakeman et al. call for a 10 points participatory checklist including NUSAP and J. R. Ravetz's process based approach

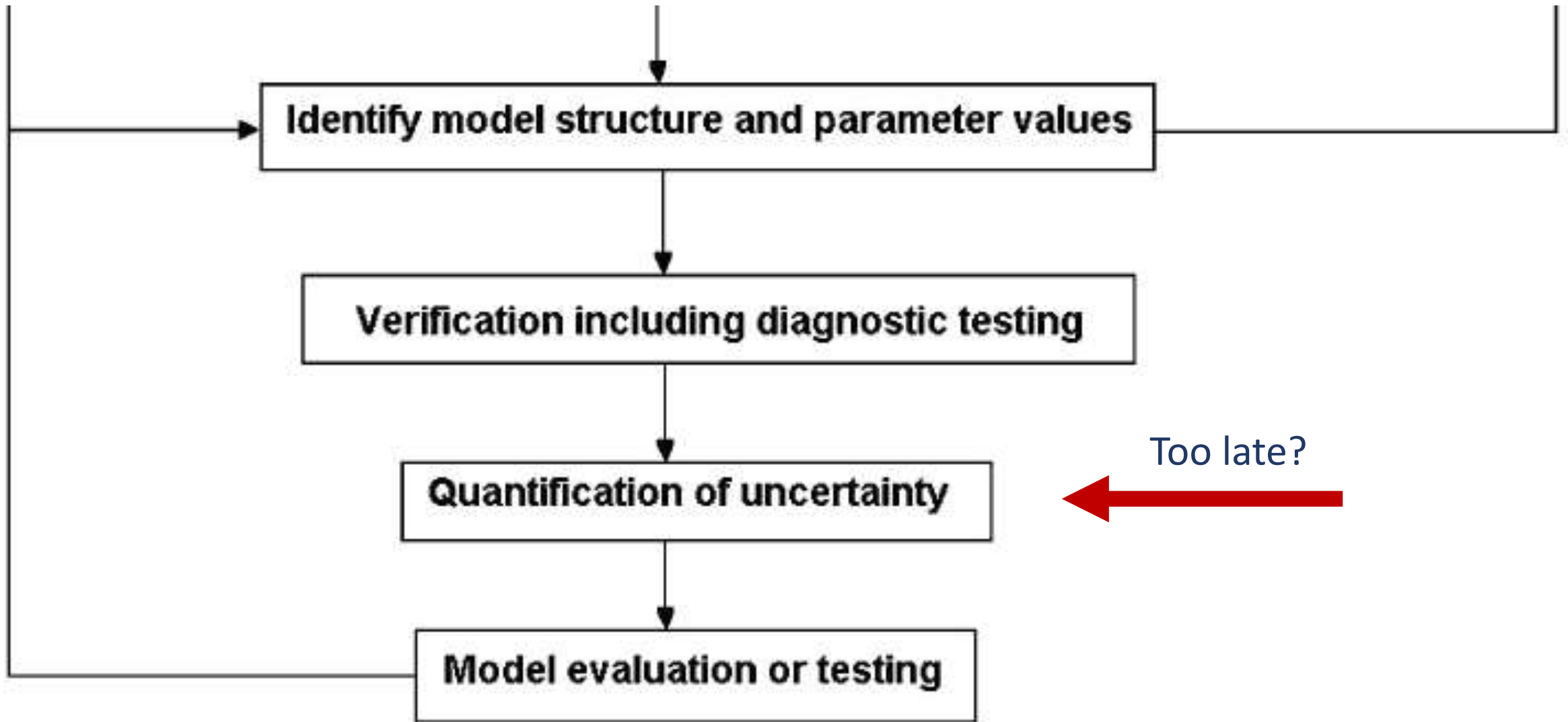
For NUSAP: Funtowicz, S.O., Ravetz, J.R., 1990. Uncertainty and Quality in Science and Policy. Kluwer, Dordrecht

J. R. Ravetz, "Integrated Environmental Assessment Forum, developing guidelines for 'good practice', Project ULYSSES.," 1997.<http://www.jvds.nl/ulysses/eWP97-1.pdf>









Start here

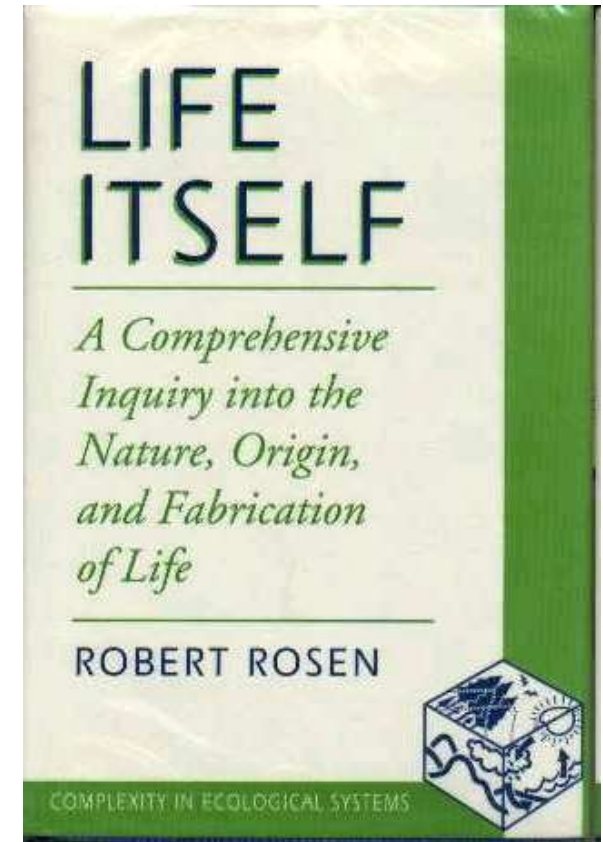
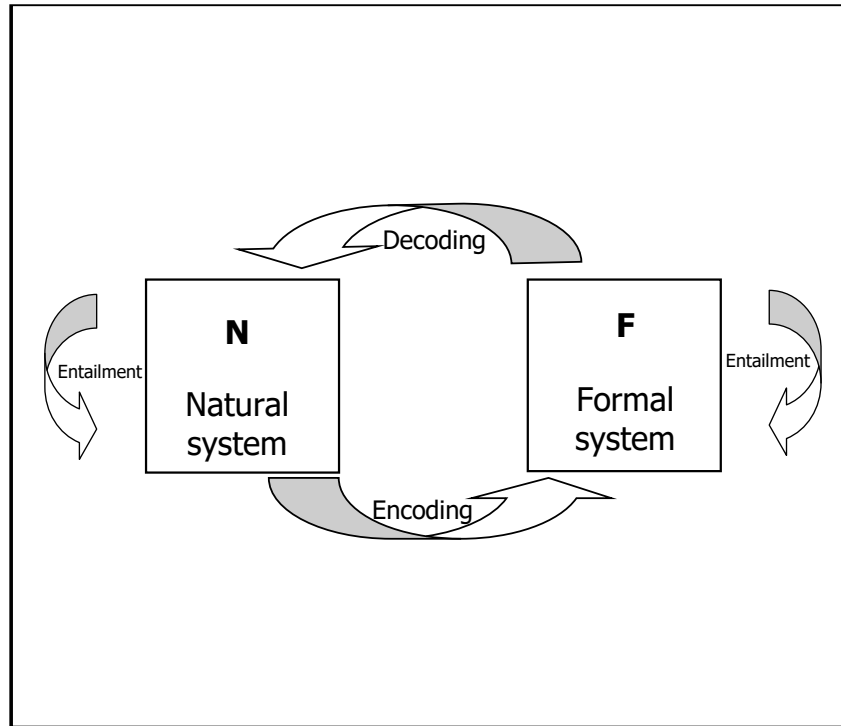
Not a discipline

Unlike statistics, mathematical modelling is not a discipline, hence the lack of universally accepted quality standards, disciplinary fora and journals and recognized leaders

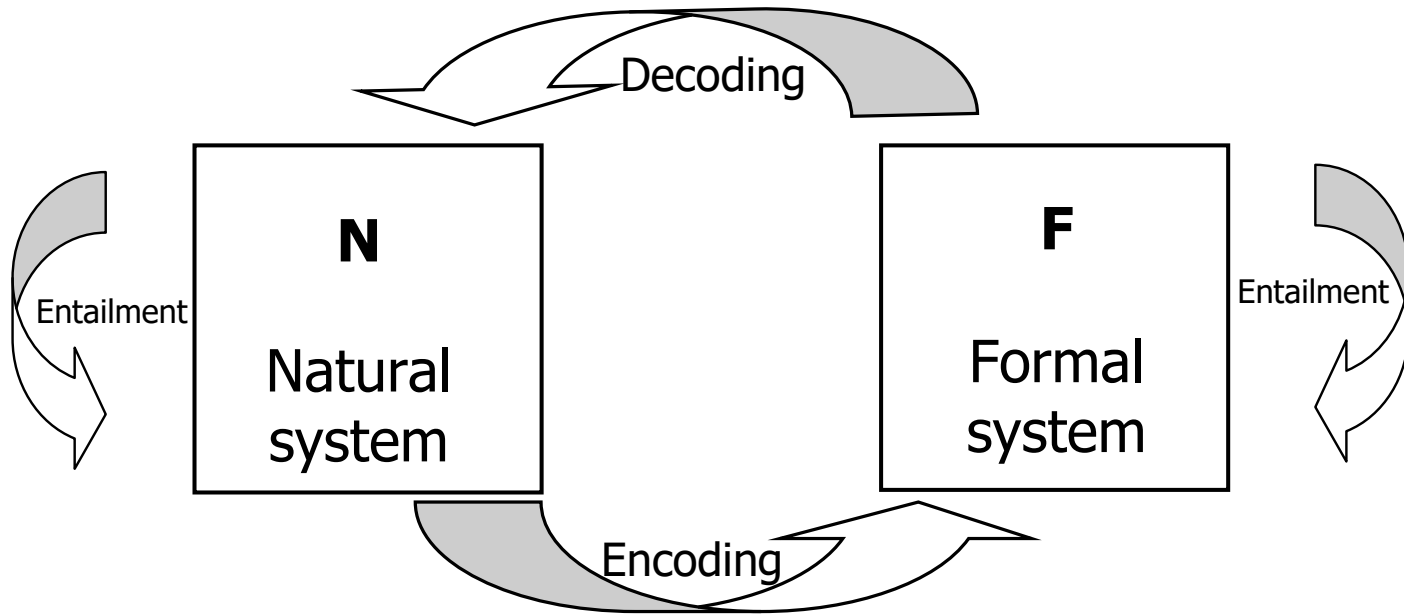
Making sensitivity analysis part of the syllabus of statistics?

Saltelli, A., Does Modelling need a reformation? Ideas for a new grammar of modelling, available at <https://arxiv.org/abs/1712.06457>

Modelling as a craft rather than as a science for Robert Rosen



R. Rosen, *Life Itself: A Comprehensive Inquiry Into the Nature, Origin, and Fabrication of Life*. Columbia University Press, 1991.



What is a model ?



Robert Rosen

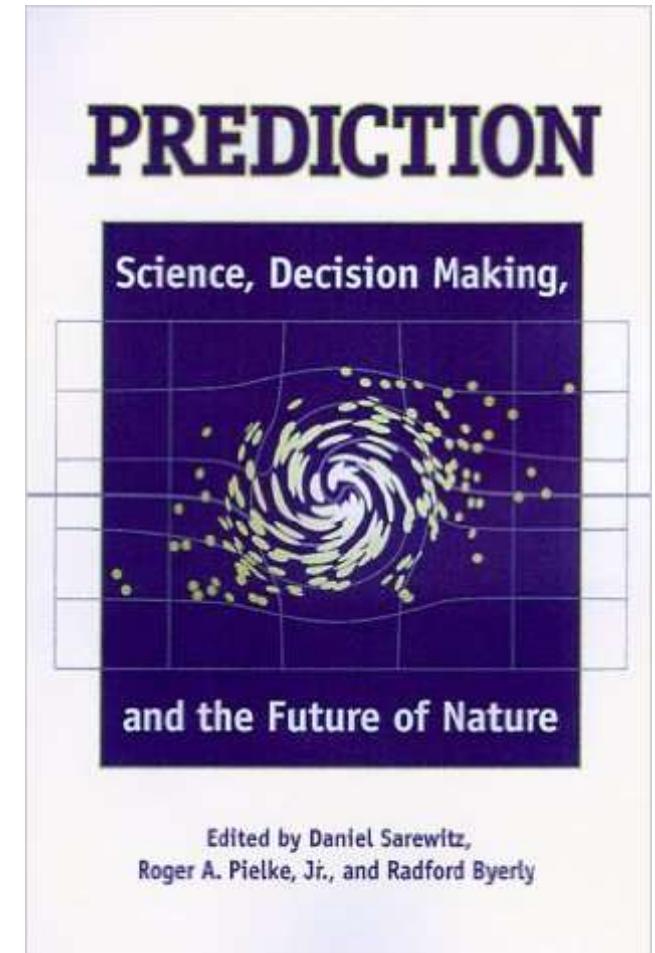
“models are most useful when they are used to challenge existing formulations, rather than to validate or verify them”



Naomi
Oreskes

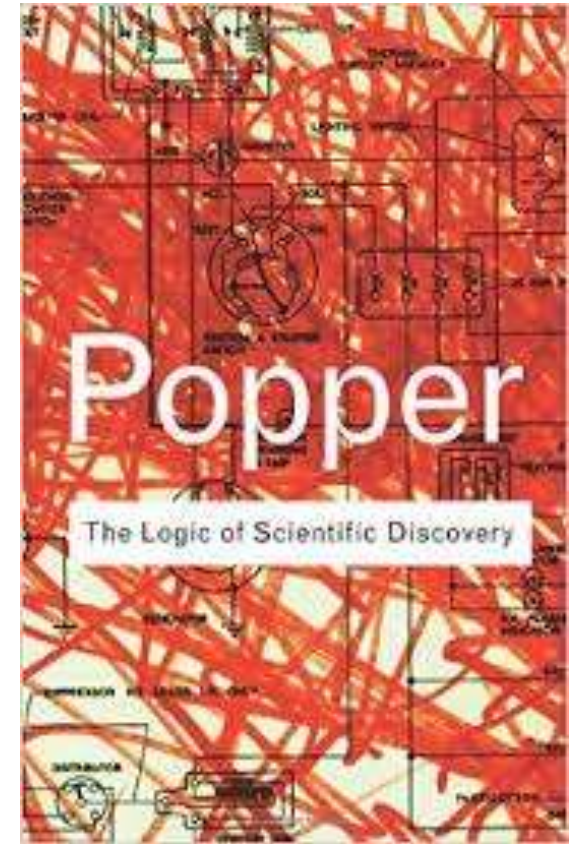
N. Oreskes, K. Shrader-Frechette, and K. Belitz, “Verification, Validation, and Confirmation of Numerical Models in the Earth Sciences,” *Science*, 263, no. 5147, 1994.

Models are not physical laws



Oreskes, N., 2000, Why predict? Historical perspectives on prediction in Earth Science, in Prediction, Science, Decision Making and the future of Nature, Sarewitz et al., Eds., Island Press, Washington DC

“ [···] to be of value in theory testing, the predictions involved must be capable of refuting the theory that generated them”
(N. Oreskes)

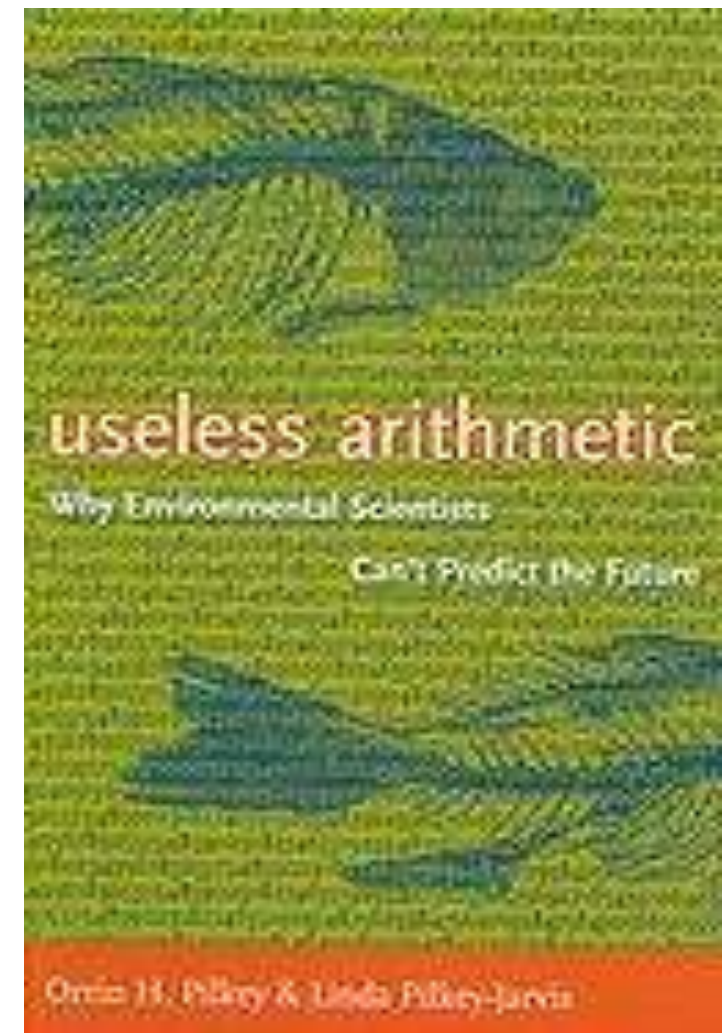


“In many cases, these temporal predictions **are treated with the same respect** that the hypothetic–deductive model of science accords to logical predictions. But this respect is largely misplaced”

“ [⋯] models are complex amalgam of theoretical and phenomenological laws (and the governing equations and algorithms that represent them), empirical input parameters, and a model conceptualization [⋯] When a model generates a prediction, of what precisely is the prediction a test? The laws? The input data? The conceptualization? Any part (or several parts) of the model might be in error, and there is no simple way to determine which one it is”

Egregious modelling failure from Pilkey and Pilkey-Jarvis

(from AIDS to coastal erosion to nuclear waste disposal ...)



O. H. Pilkey and L. Pilkey-Jarvis, *Useless Arithmetic: Why Environmental Scientists Can't Predict the Future*. Columbia University Press, 2009.

For John Kay modelling may need as input information which we don't have (The case of WEBTAG; knowing car passengers number decades into futures)

John Kay



J. A. Kay, "Knowing when we don't know," 2012,
https://www.ifs.org.uk/docs/john_kay_feb2012.pdf

WebTAG: Annual Percentage Change in Car Occupancy (% pa) up to 2036

| Journey Purpose | Weekday | | | | | Weekend | All Week |
|-------------------------------------|----------|----------|---------|---------|-----------------|---------|----------|
| | 7am-10am | 10am-4pm | 4pm-7pm | 7pm-7am | Weekday Average | | |
| Work | -0.48 | -0.4 | -0.62 | -0.5 | -0.44 | -0.48 | -0.45 |
| Non - Work (commuting and other) | -0.67 | -0.65 | -0.53 | -0.47 | -0.59 | -0.52 | -0.56 |

Paul Romer's Mathiness = use of
mathematics to veil normative stances

Erik Reinert: scholastic tendencies in the
mathematization of economics

P. M. Romer, "Mathiness in the Theory of Economic Growth," *Am. Econ. Rev.*, vol. 105, no. 5, pp. 89–93, May 2015.

E. S. Reinert, "Full circle: economics from scholasticism through innovation and back into mathematical scholasticism," *J. Econ. Stud.*, vol. 27, no. 4/5, pp. 364–376, Aug. 2000.

Uncertainty and sensitivity analysis

Definitions

Uncertainty analysis: Focuses on just quantifying the uncertainty in model output

Sensitivity analysis: The study of the relative importance of different input factors on the model output

Why Sensitivity analysis?

European Commission, 2015

Office for the Management and Budget, 2006

Environmental Protection Agency, 2009

EPA, 2009, March. Guidance on the Development, Evaluation, and Application of Environmental Models. Technical Report EPA/100/K-09/003. Office of the Science Advisor, Council for Regulatory Environmental Modeling, <http://nepis.epa.gov/Exe/ZyPDF.cgi?Dockey=P1003E4R.PDF>, Last accessed December 2015.

EUROPEAN COMMISSION, Better regulation toolbox, appendix to the Better Regulation Guidelines, Strasbourg, 19.5.2015, SWD(2015) 111 final, COM(2015) 215 final, http://ec.europa.eu/smart-regulation/guidelines/docs/swd_br_guidelines_en.pdf.

OMB, Proposed risk assessment bulletin, Technical report, The Office of Management and Budget's – Office of Information and Regulatory Affairs (OIRA), January 2006, https://www.whitehouse.gov/sites/default/files/omb/assets/omb/inforeg/proposed_risk_assessment_bulletin_010906.pdf, pp. 16–17, accessed December 2015.

<http://ec.europa.eu/smart-regulation/>



The screenshot shows the 'Better Regulation Guidelines' page on the European Commission website. The page features a blue header with the European Commission logo and the text 'Better Regulation'. Below the header is a navigation menu with options like Home, REFIT, Stakeholder consultations, Roadmaps / Inception Impact Assessments, Impact Assessment, Evaluation, Regulatory Scrutiny Board, and Guidelines. The main content area is titled 'Better Regulation Guidelines' and contains text explaining the guidelines, their structure, and their basis in public consultation exercises. A sidebar on the right includes a search bar, social media links, latest documents, and a feedback form.

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European Commission

Better Regulation

European Commission > Better Regulation > Guidelines

Home

REFIT

Stakeholder consultations

Roadmaps / Inception Impact Assessments

Impact Assessment

Evaluation

Regulatory Scrutiny Board

Guidelines

- Better Regulation Guidelines
- Better Regulation "Toolbox"
- Key documents

Better Regulation Guidelines

These guidelines explain what Better Regulation is and how it should be applied in the day to day practices when preparing new initiatives and proposals or managing existing policies and legislation.

They cover the whole policy cycle, from policy preparation and adoption to implementation and application, to evaluation and revision of EU law. For each of these phases there are a number of Better Regulation principles, objectives, tools and procedures to make sure that the EU has the best regulation possible. These relate to planning, impact assessment, stakeholder consultation, implementation and evaluation.

The [Better Regulation Guidelines](#) are structured into chapters which cover each of the instruments of the law-making process. The corresponding [toolbox](#) gives more detailed and technical information.

Better Regulation Guidelines are based on the outcomes of public consultation exercises carried out in 2013 and 2014.

- [Public consultation on the revision of the Commission's Impact Assessment Guidelines](#)
- [Stakeholder Consultation Guidelines](#)
- [Consultation on the draft Commission Evaluation Policy Guidelines](#)

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- 19/05/2015 - Better Regulation Package

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Source: IA Toolbox, p. 391



4. SENSITIVITY AND UNCERTAINTY ANALYSES

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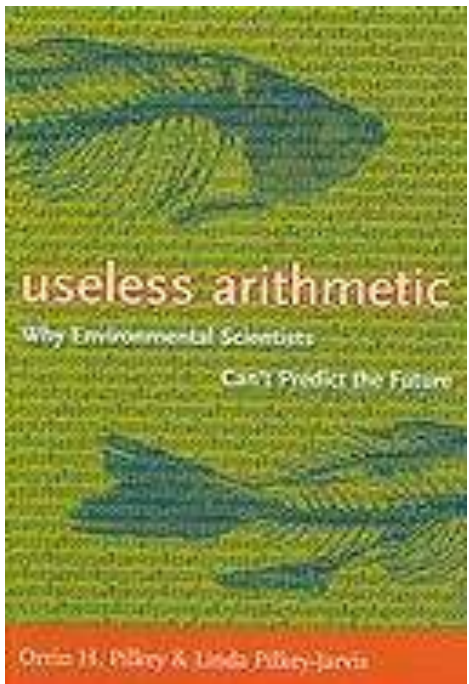
Six steps for a global SA:

1. Select one output of interest;
2. Participatory step: discuss which input may matter;
3. Participatory step (extended peer review): define distributions;
4. Sample from the distributions;
5. Run (=evaluate) the model for the sampled values;
6. Obtain in this way both the uncertainty of the prediction and the relative importance of variables.

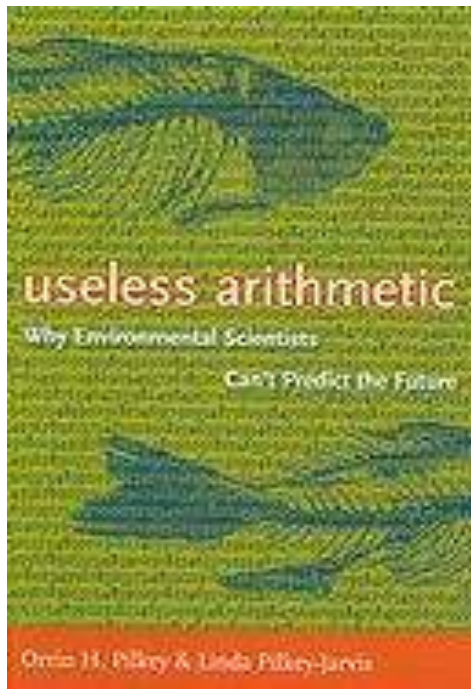
Limits of sensitivity analysis



Orrin H.
Pilkey



Useless Arithmetic: Why
Environmental Scientists Can't
Predict the Future
by Orrin H. Pilkey and Linda
Pilkey-Jarvis

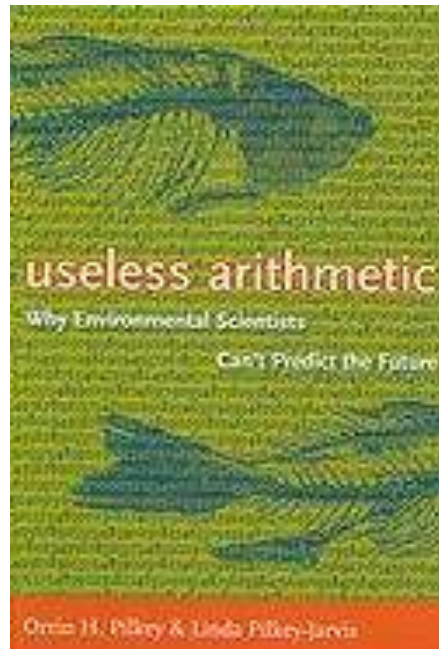


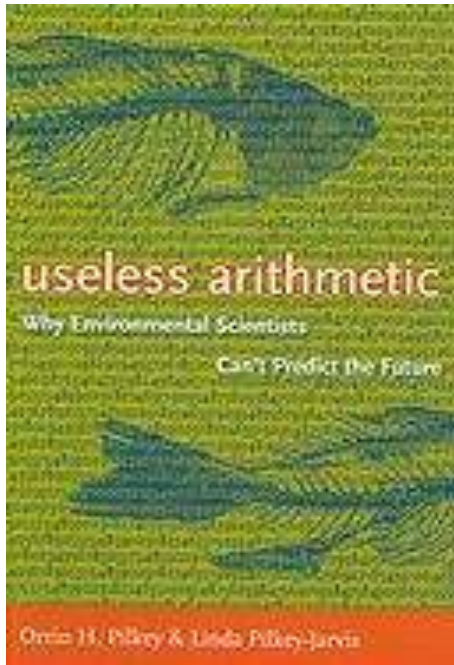
<<It is important, however, to recognize that the sensitivity of the parameter in the equation is what is being determined, not the sensitivity of the parameter in nature.

[...] If the model is wrong or if it is a poor representation of reality, determining the sensitivity of an individual parameter in the model is a meaningless pursuit.>>

One of the examples discussed concerns the **Yucca Mountain** repository for radioactive waste. TSPA model (for total system performance assessment) for safety analysis.

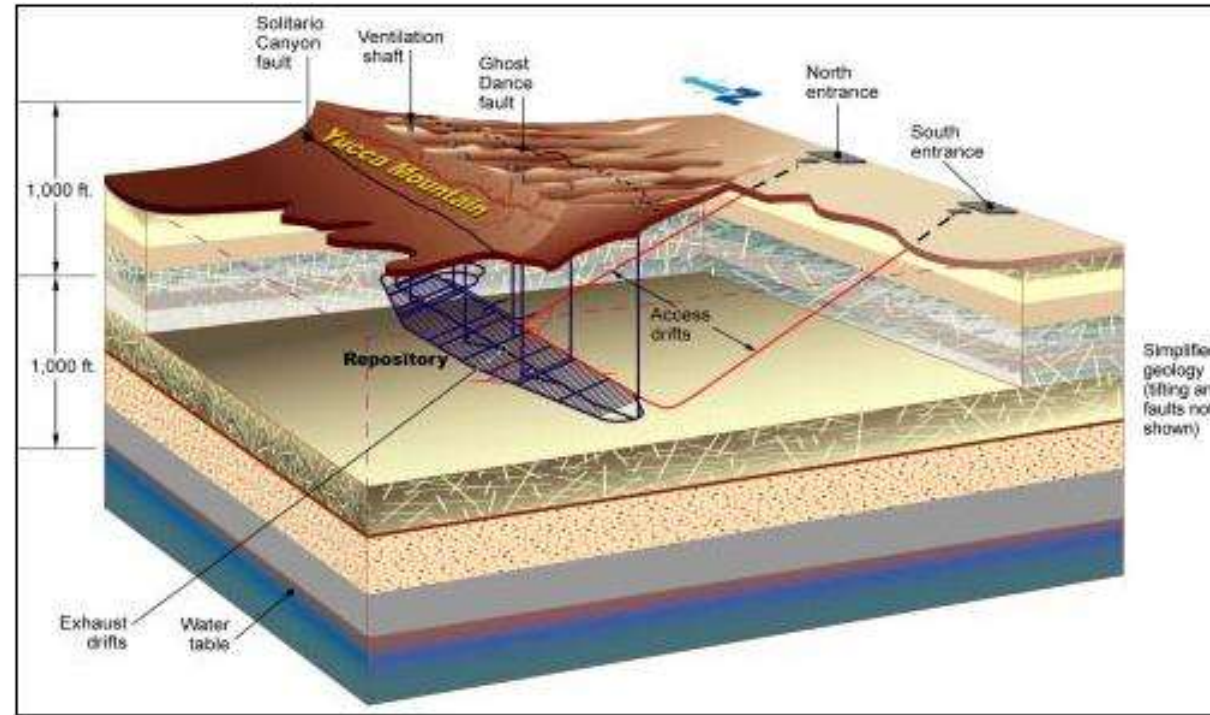
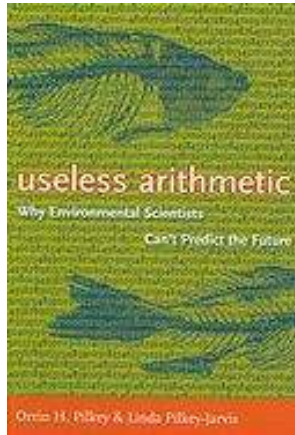
TSPA is Composed of 286 sub-models.





TSPA (like any other model) **relies on assumptions** → one is the low permeability of the geological formation → long time for the water to percolate from surface to disposal.



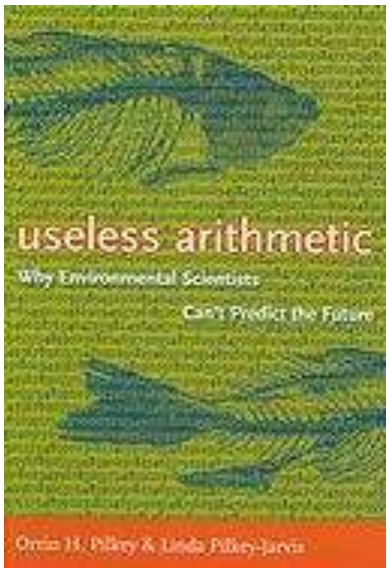


The confidence of the stakeholders in TSPA was not helped when evidence was produced which could lead to an upward revision of 4 orders of magnitude of this parameter
(the ^{36}Cl story)

Type III error in sensitivity:
Examples:

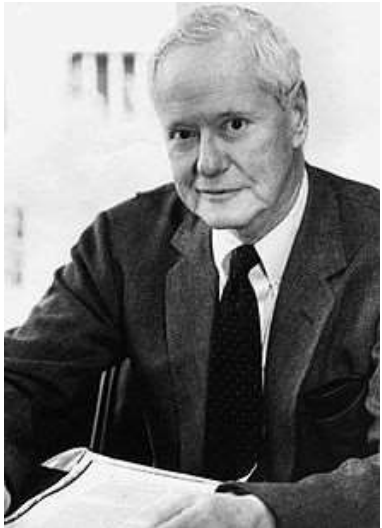
In the case of TSPA (Yucca mountain) a range of 0.02 to 1 millimetre per year was used for percolation of flux rate.

→... SA useless if it is instead ~ 3,000 millimetres per year.



“Scientific mathematical modelling should involve constant efforts to falsify the model”

Ref. → Robert K. Merton’s ‘Organized skepticism’



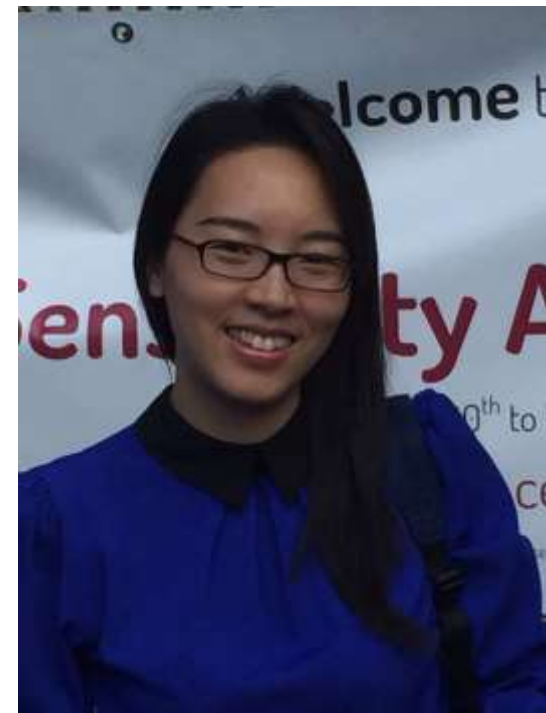
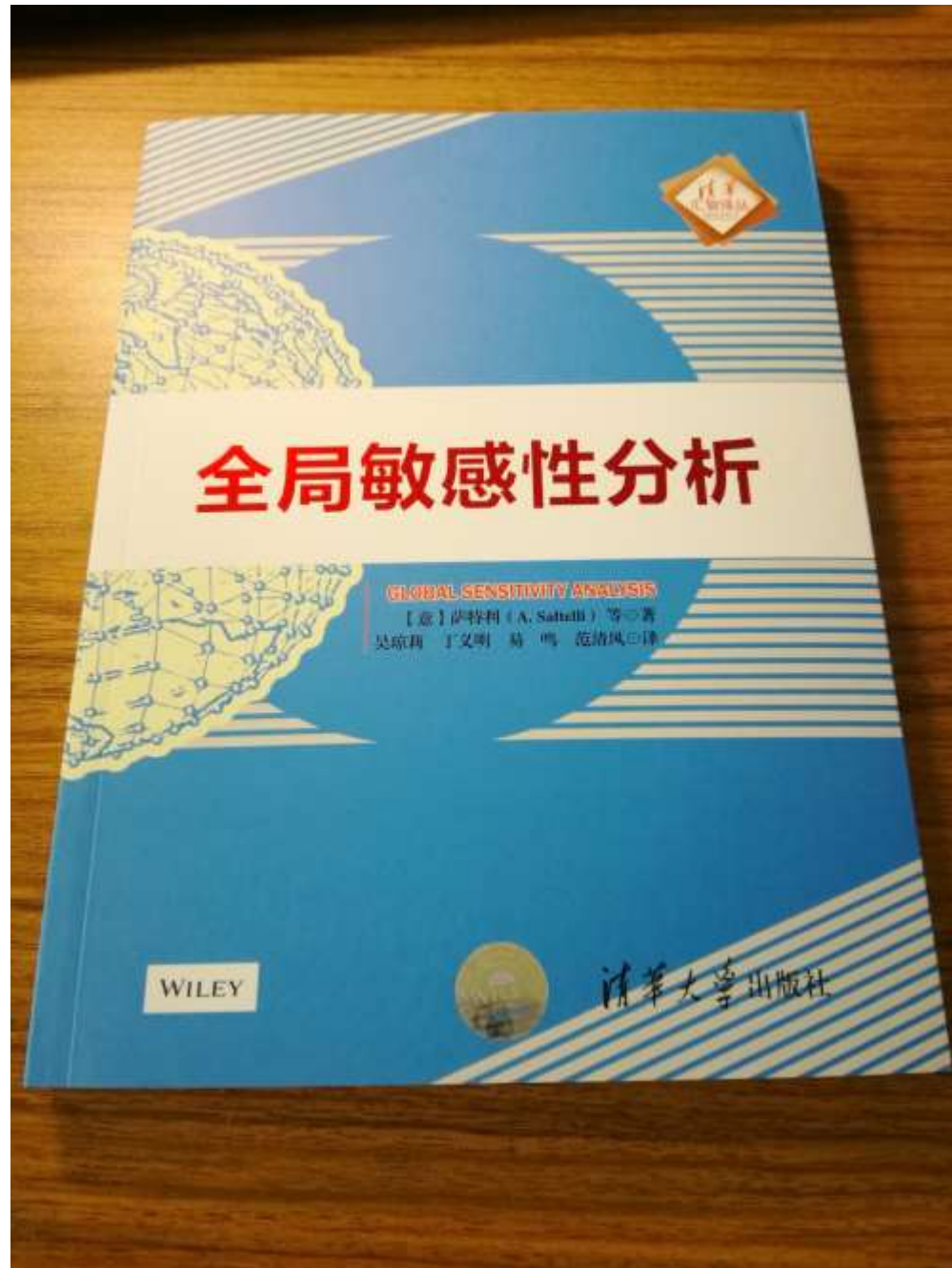
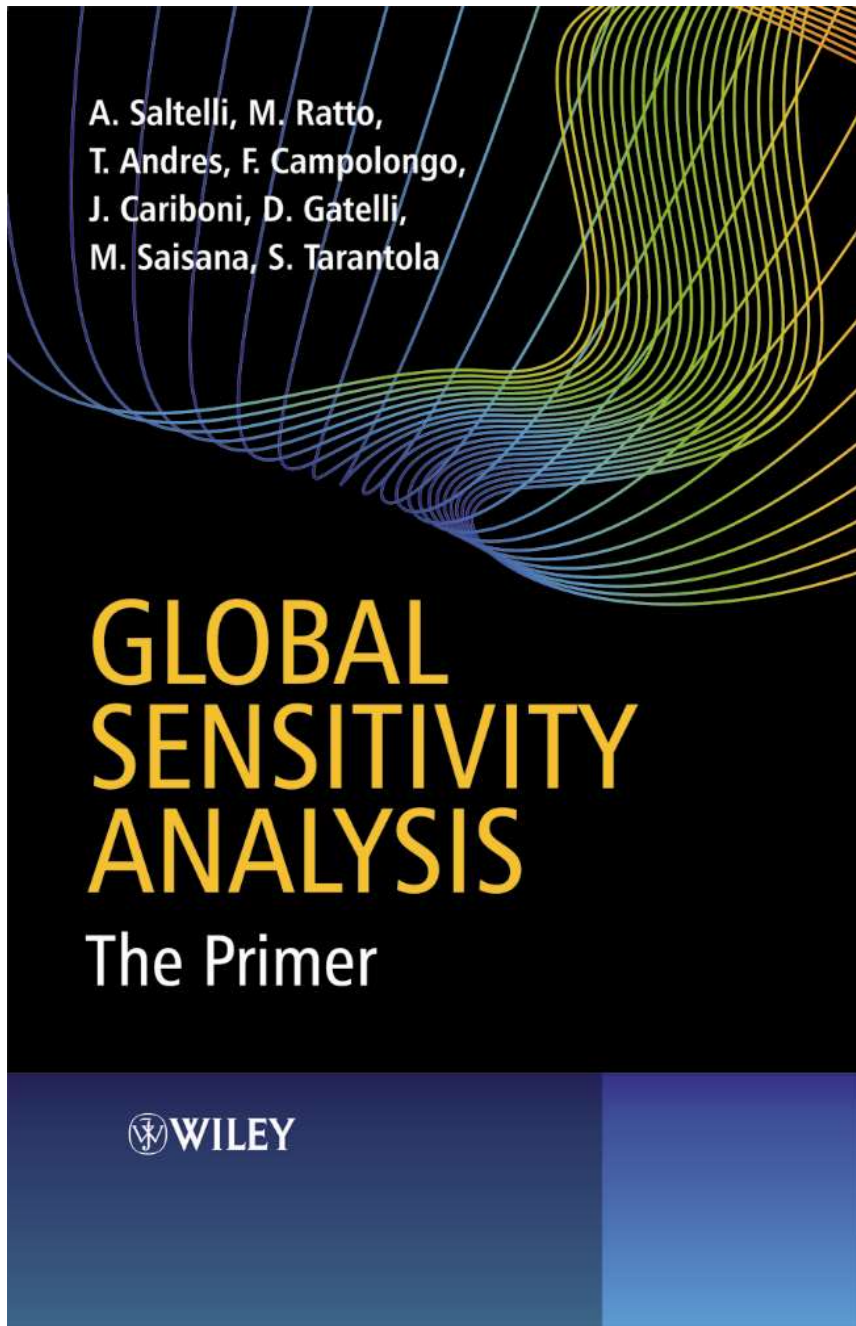
Robert K. Merton

Communalism – the common ownership of scientific discoveries, according to which scientists give up intellectual property rights in exchange for recognition and esteem (Merton actually used the term Communism, but had this notion of communalism in mind, not Marxism);

Universalism – according to which claims to truth are evaluated in terms of universal or impersonal criteria, and not on the basis of race, class, gender, religion, or nationality;

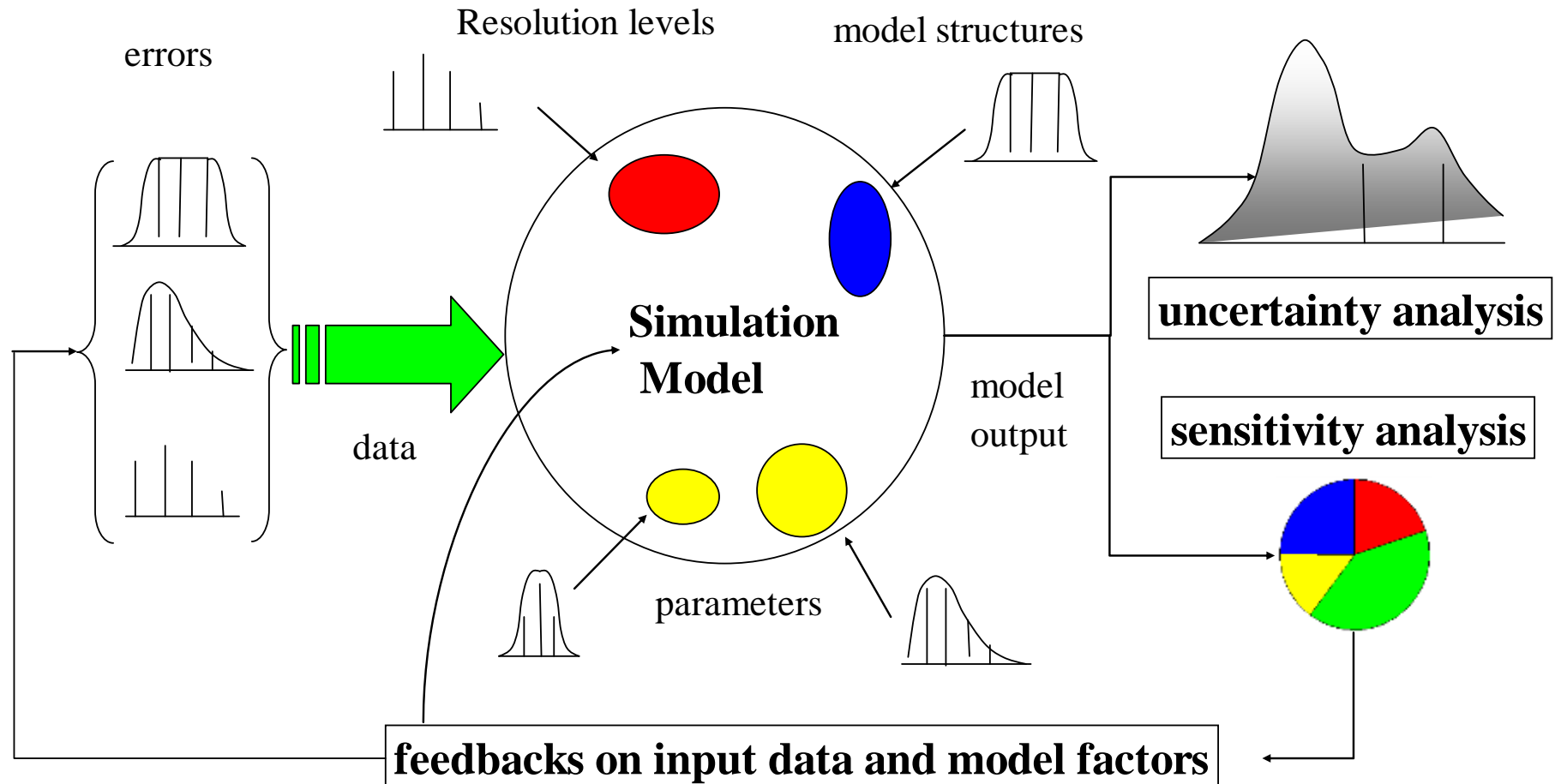
Disinterestedness – according to which scientists are rewarded for acting in ways that outwardly appear to be selfless;

Organized Skepticism – all ideas must be tested and are subject to rigorous, structured community scrutiny.



Wu
Qiongli

An engineer's vision of UA, SA

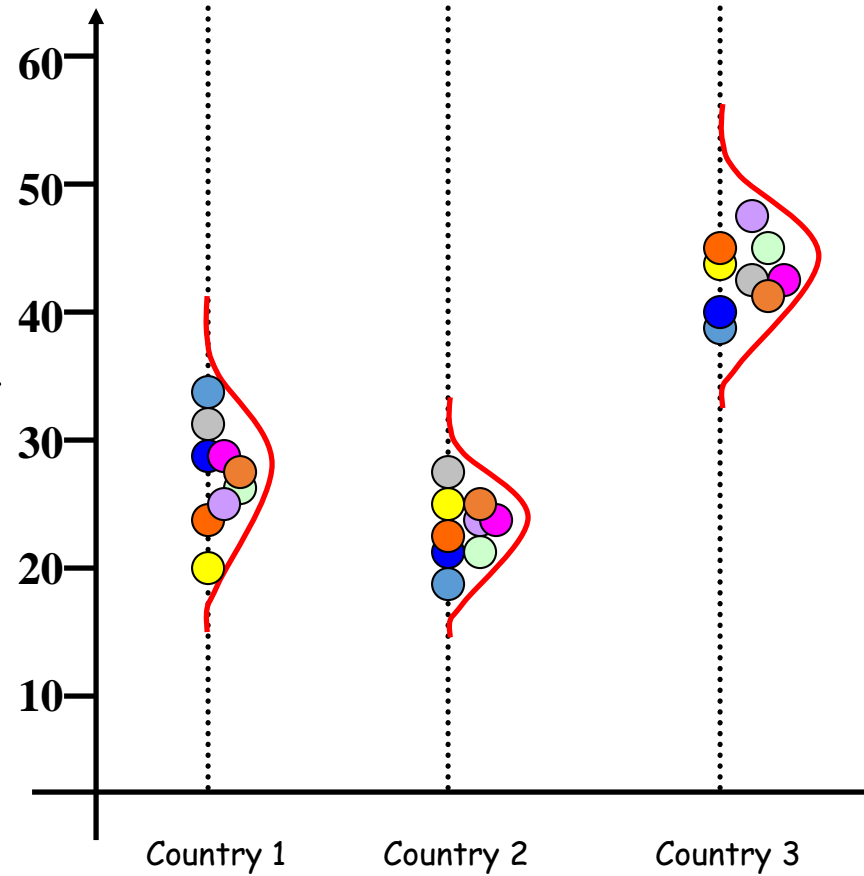
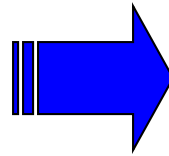
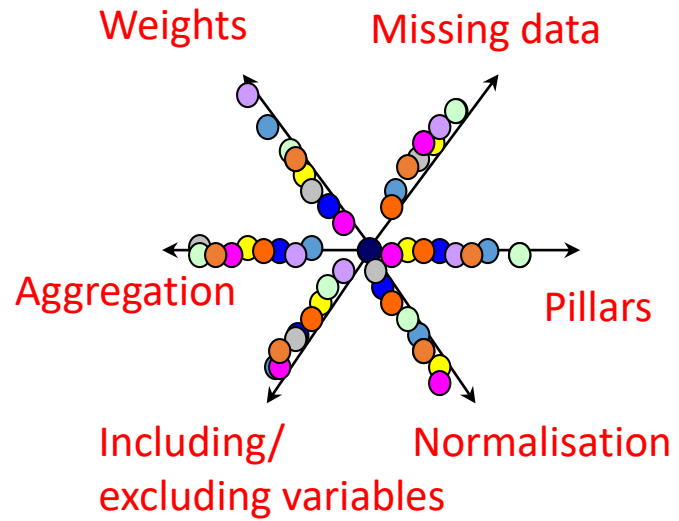


One can sample more than just factors

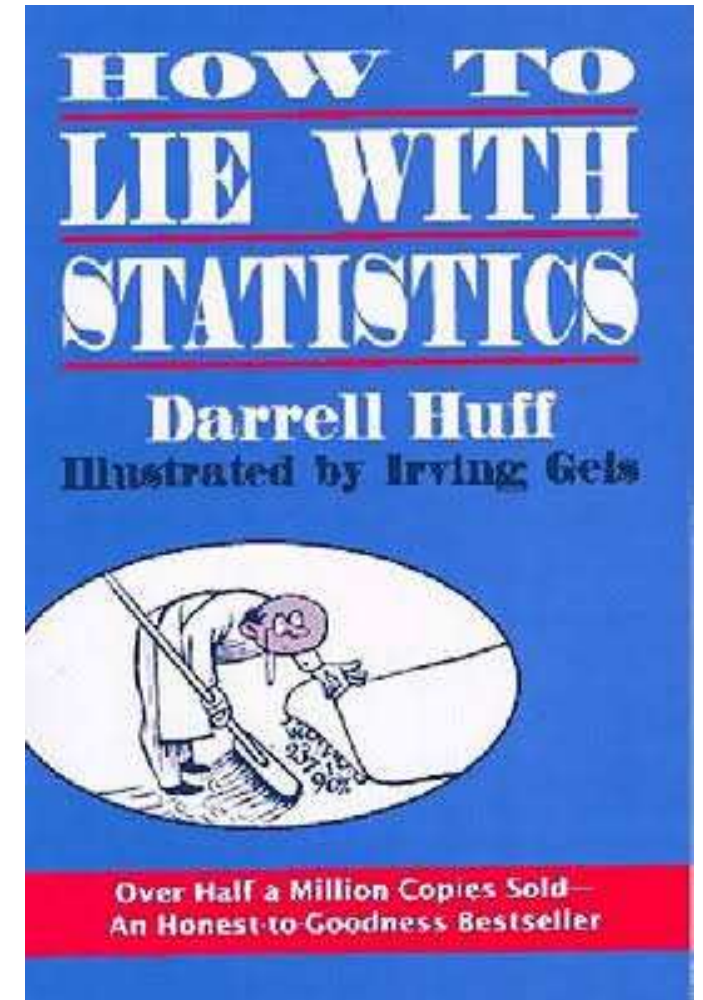
One can sample modelling assumptions,
alternative data sets, resolution levels,
scenarios ...

| Assumption | Alternatives |
|----------------------|--|
| Number of indicators | <ul style="list-style-type: none">▪ all six indicators included or one-at-time excluded (6 options) |
| Weighting method | <ul style="list-style-type: none">▪ original set of weights,▪ factor analysis,▪ equal weighting,▪ data envelopment analysis |
| Aggregation rule | <ul style="list-style-type: none">▪ additive,▪ multiplicative,▪ Borda multi-criterion |

Space of alternatives

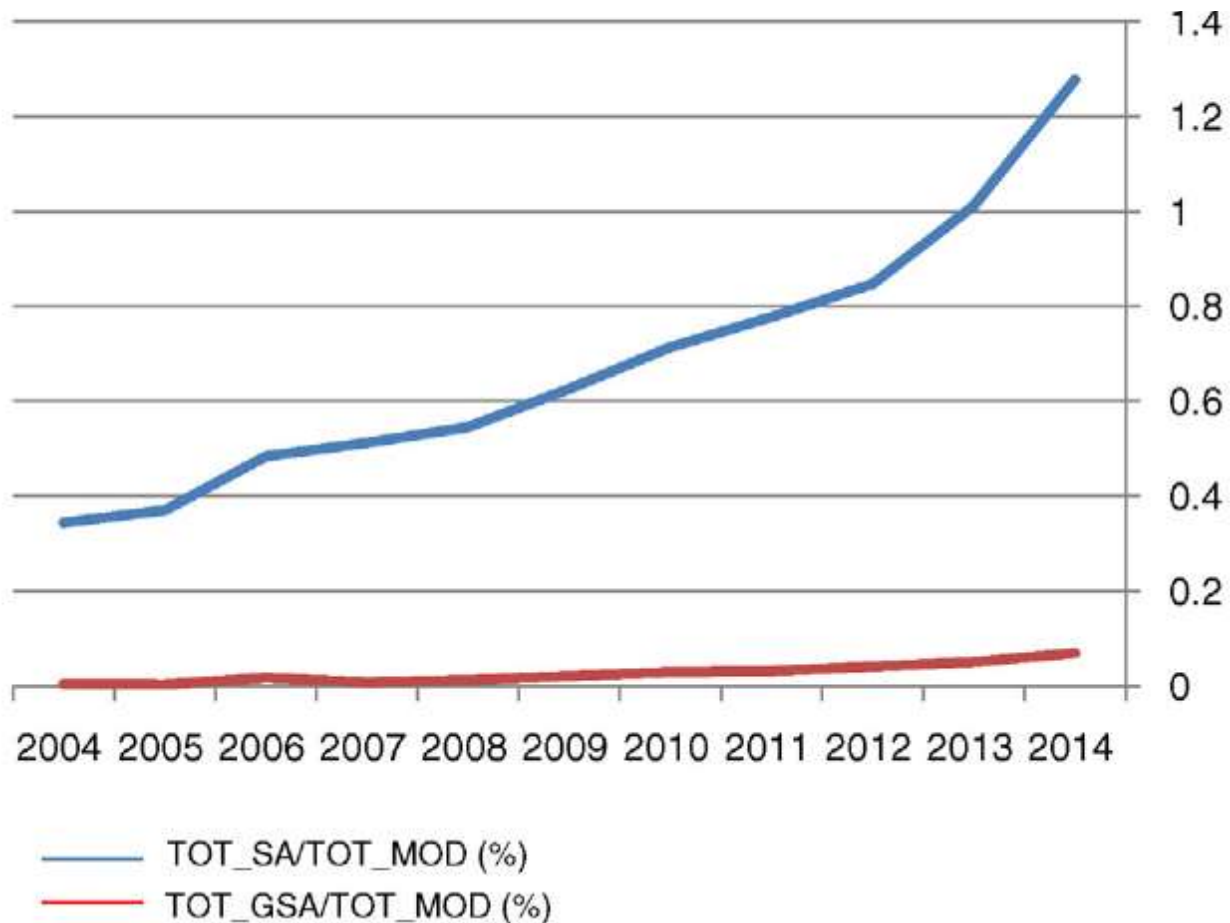


Can one lie with sensitivity analysis as one can lie with statistics?



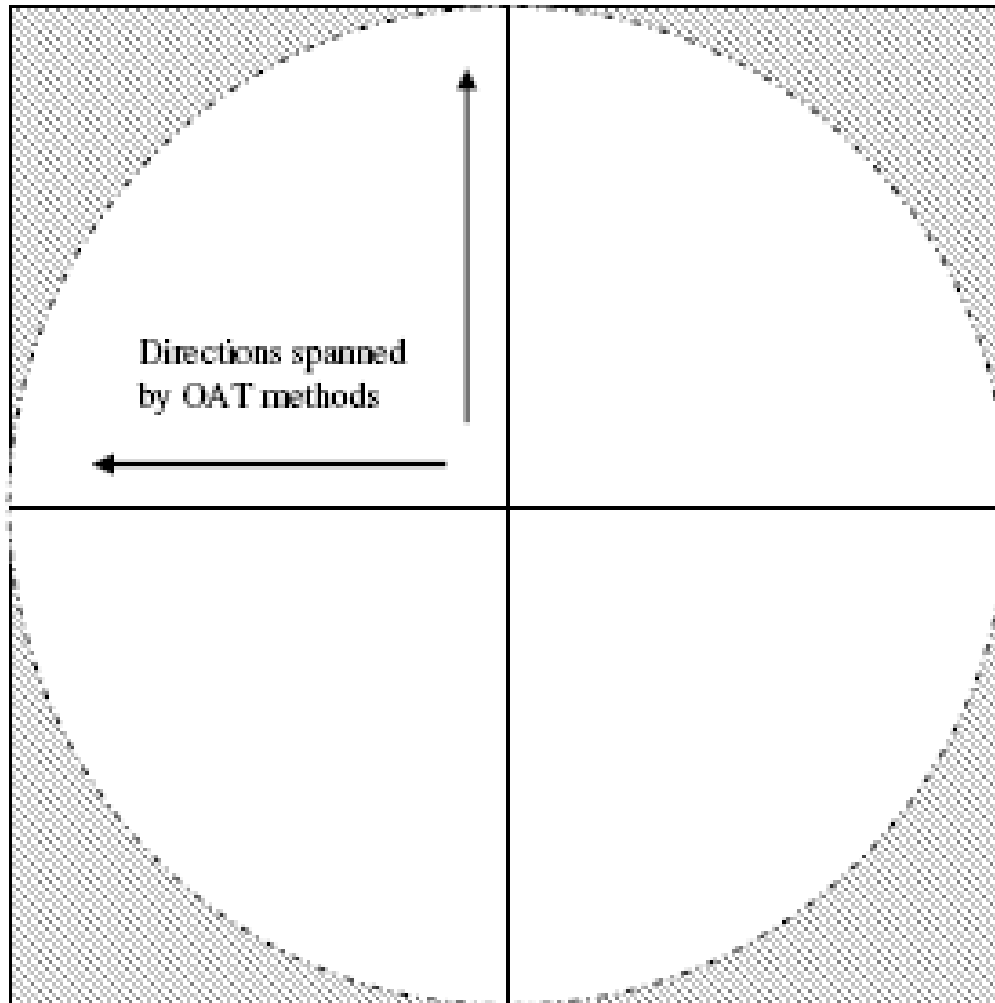
Saltelli, A., Annoni P., 2010, How to avoid a perfunctory sensitivity analysis, Environmental Modeling and Software, 25, 1508–1517.

In 2014 out of 1000 papers in modelling 12 have a sensitivity analysis and < 1 a global SA; most SA still move one factor at a time



Ferretti, F., Saltelli A., Tarantola, S., 2016, Trends in Sensitivity Analysis practice in the last decade, Science of the Total Environment, <http://dx.doi.org/10.1016/j.scitotenv.2016.02.133>

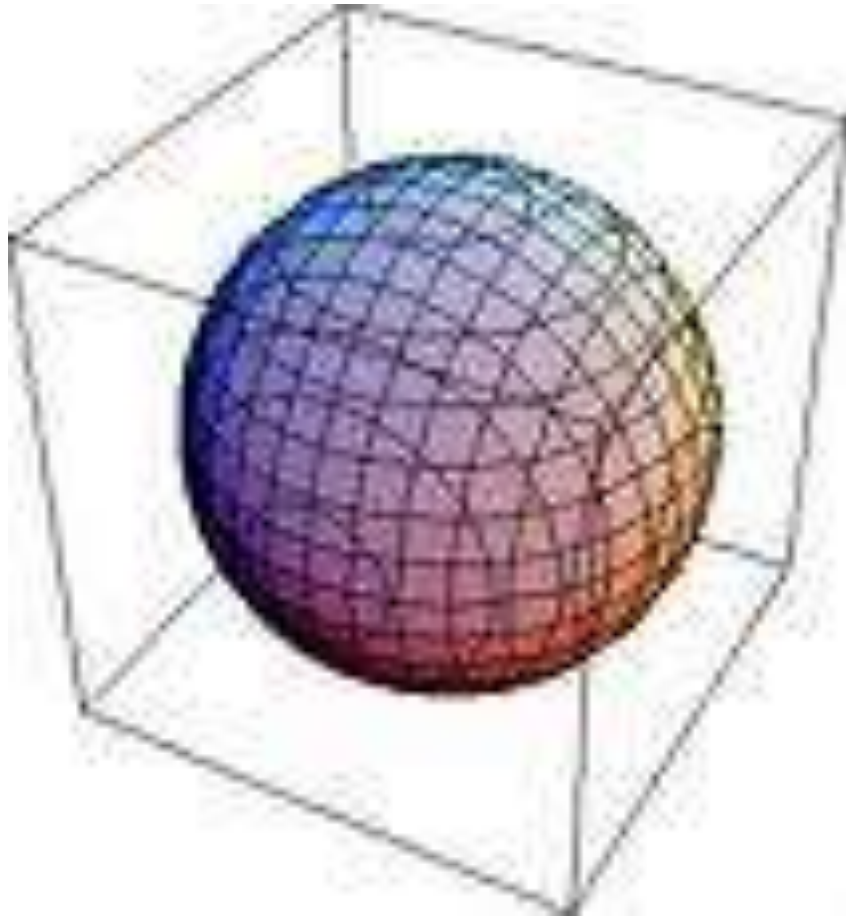
OAT in 2 dimensions



Area circle
/ area
square = ?

$\sim 3/4$

OAT in 3 dimensions



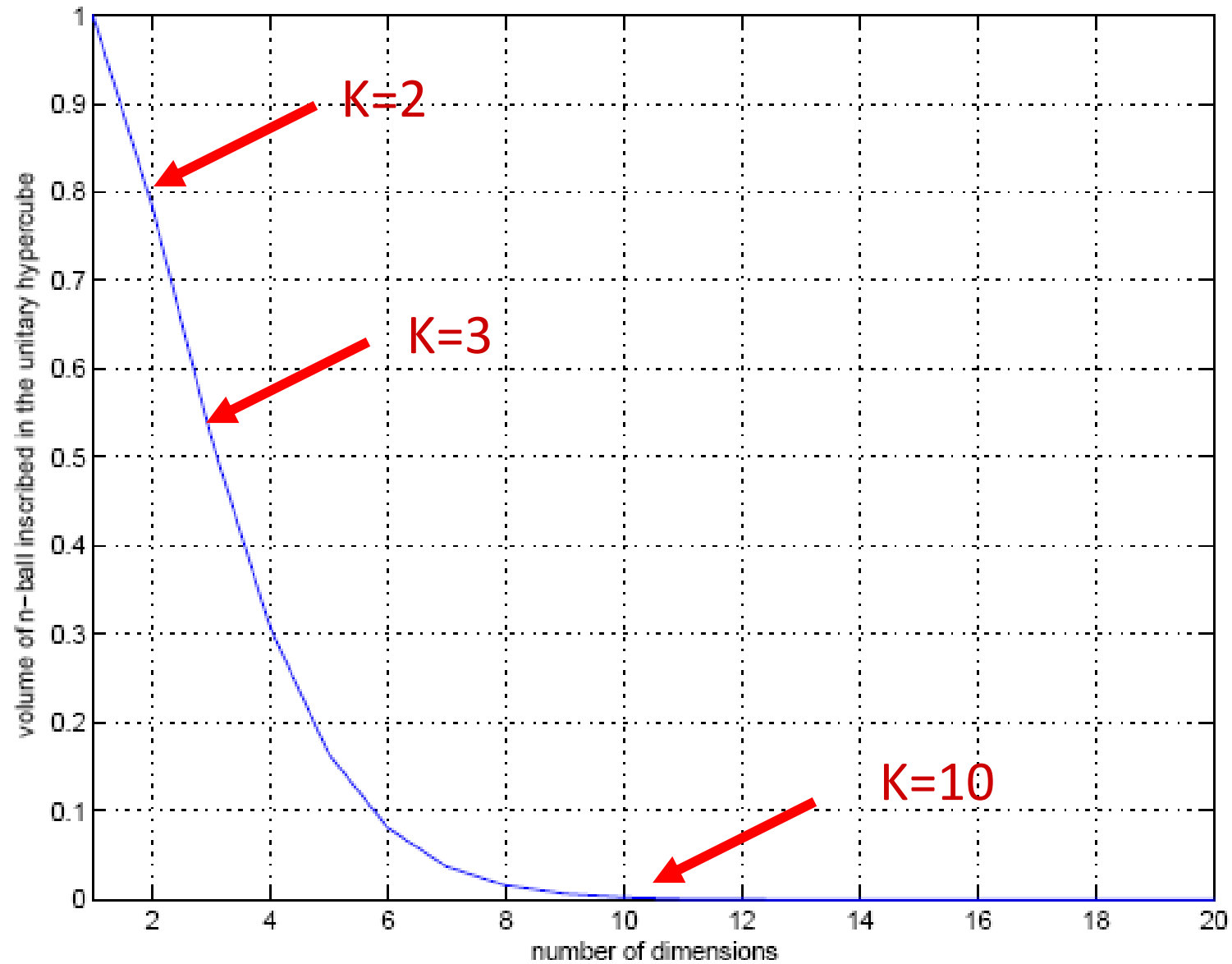
Volume sphere /
volume cube = ?

~ 1/2

OAT in 10 dimensions; Volume
hypersphere / volume ten dimensional
hypercube =? ~ 0.0025

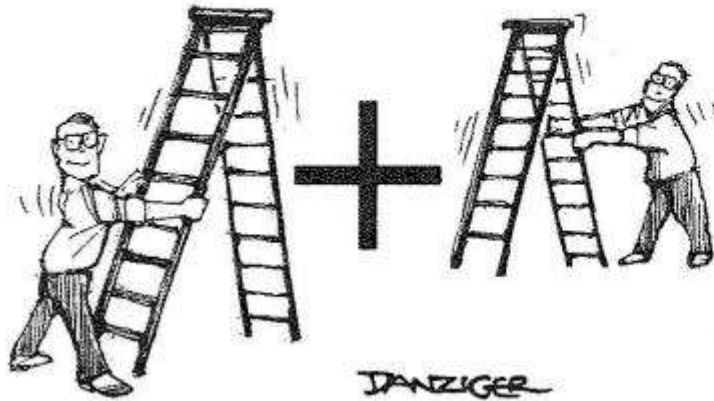


OAT in k dimensions



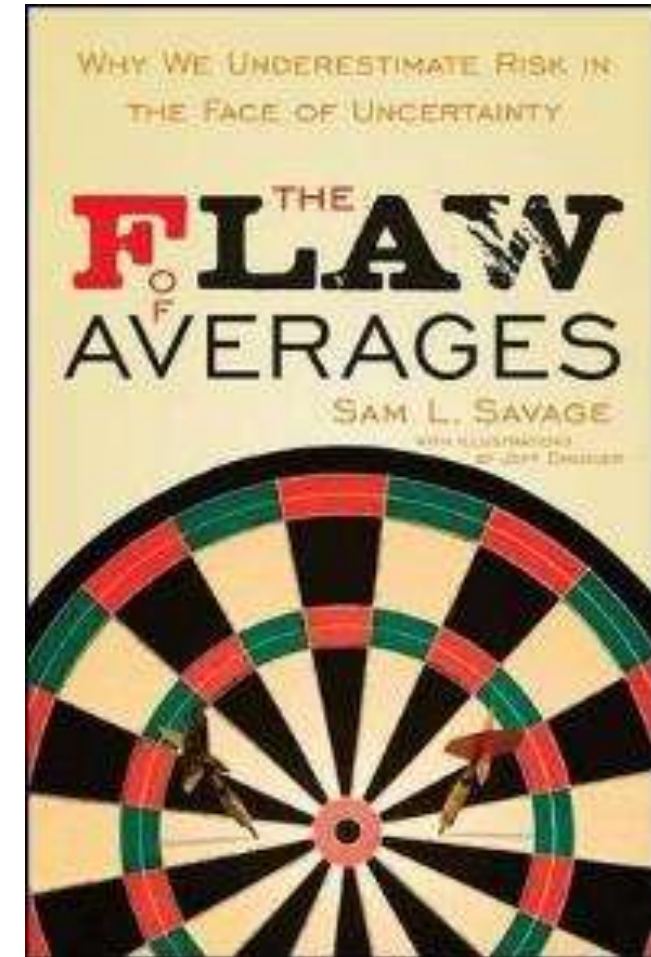
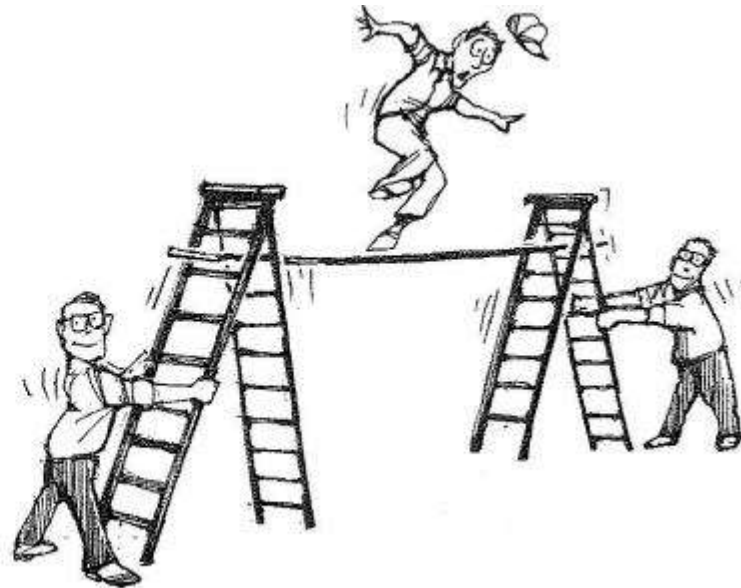
How would you test the scaffolding?

How coupled ladders are shaken in most of available literature



≠

How to shake coupled ladders

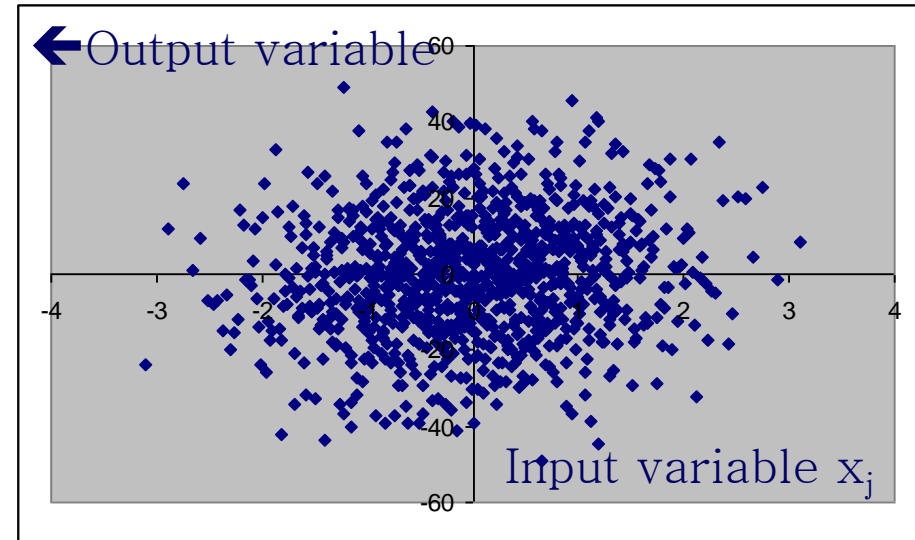
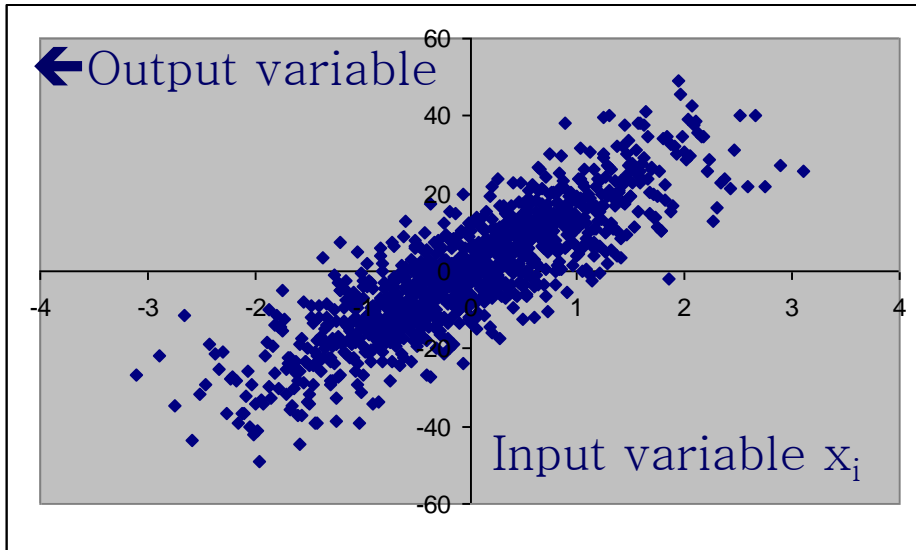


Once a sensitivity analysis is done via OAT there is no guarantee that either uncertainty analysis (UA) or sensitivity analysis (SA) will be any good:

→ UA will be non conservative

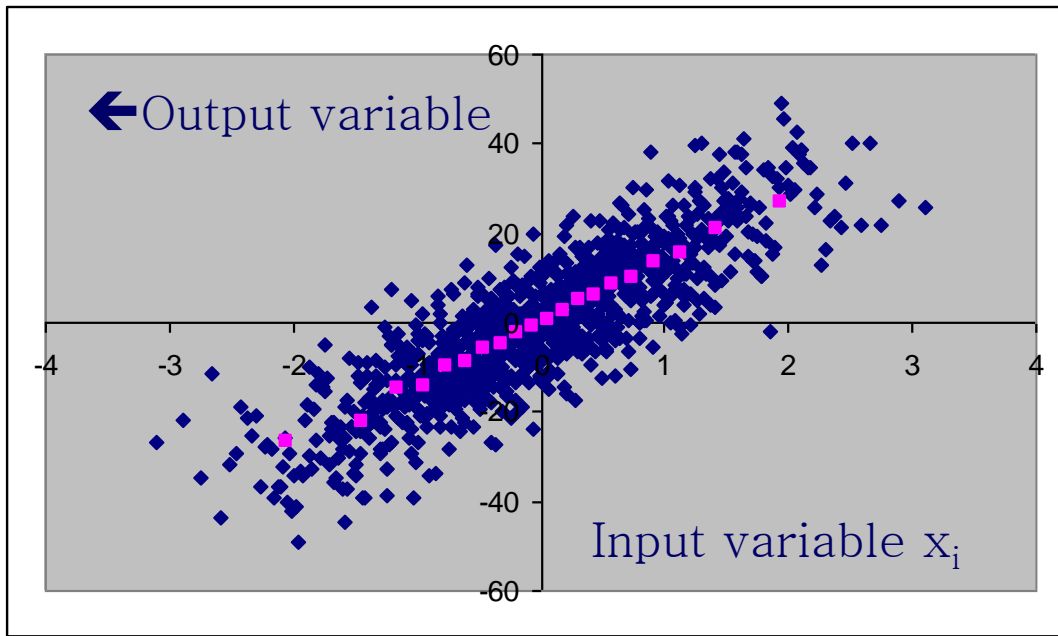
→ SA may miss important factors

Stop here



Which factor is more important?

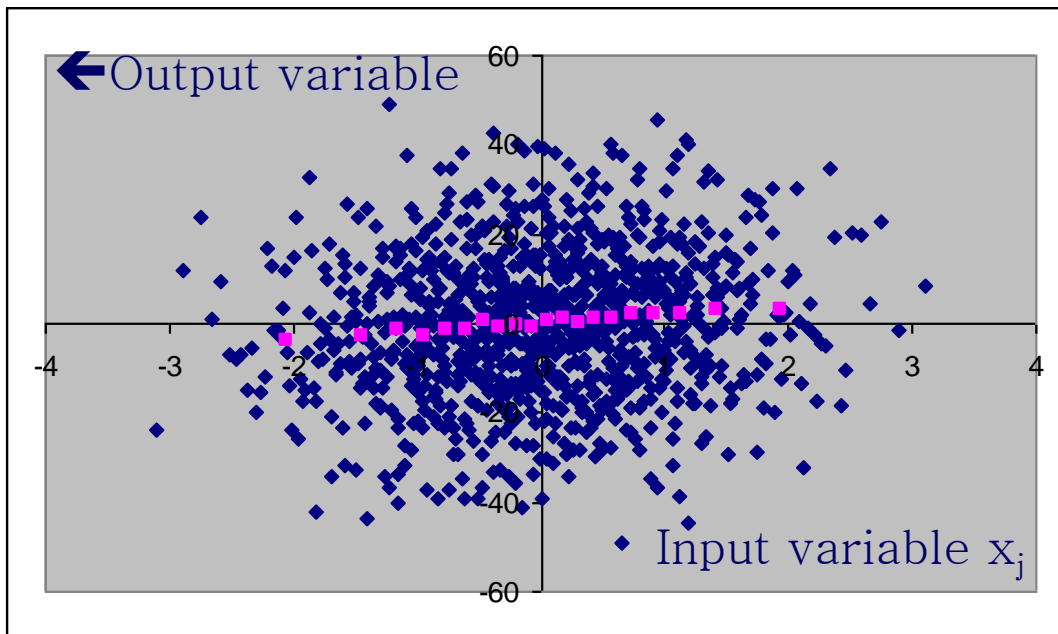
Why?

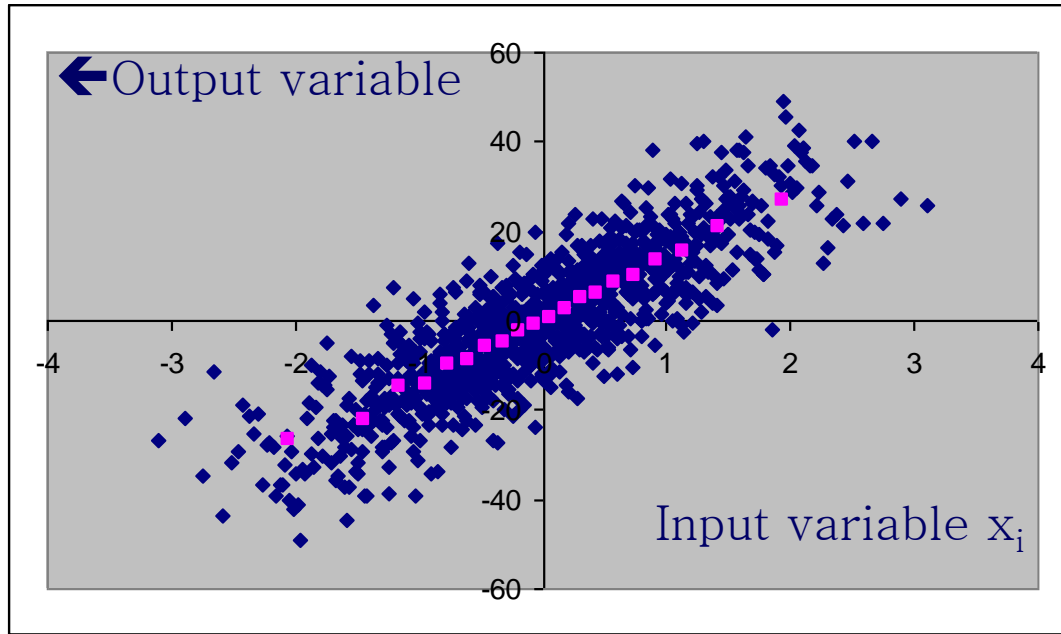


~1,000 blue points

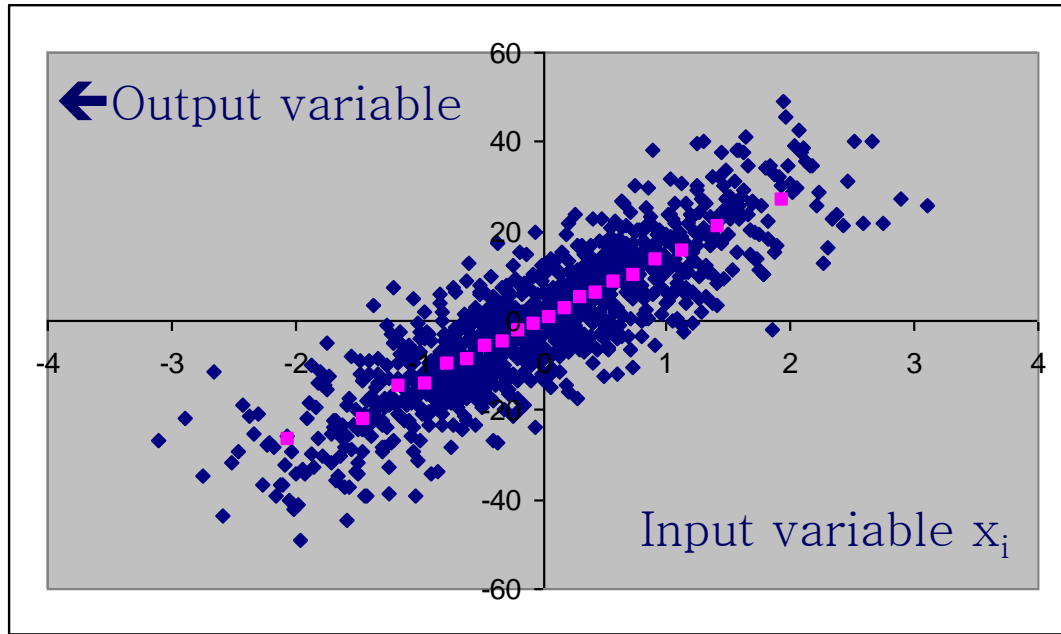
Divide them in 20 bins of ~ 50 points

Compute the bin's average (pink dots)



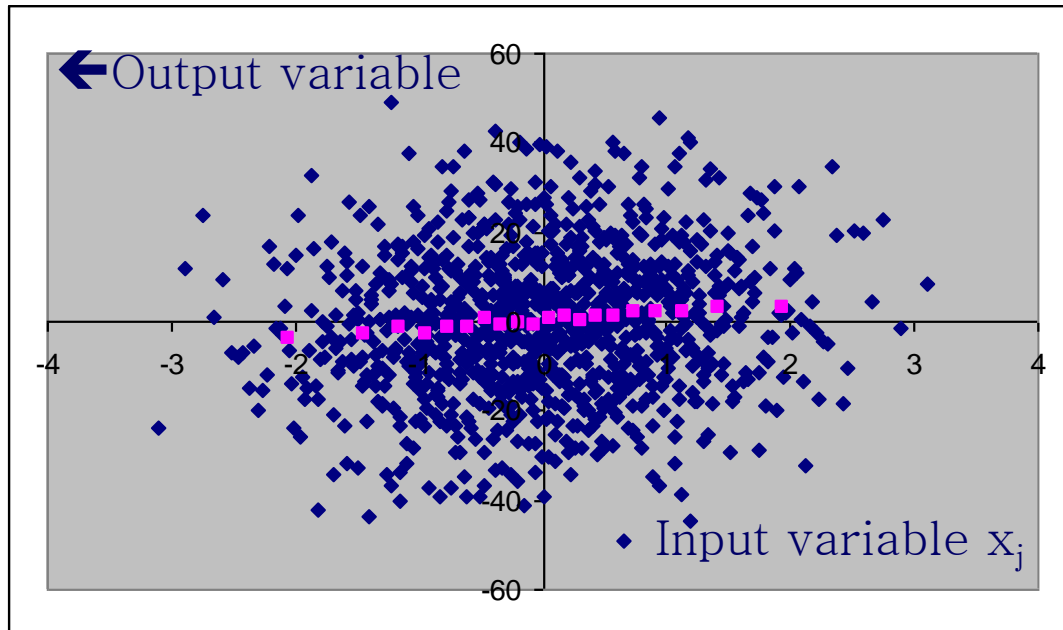
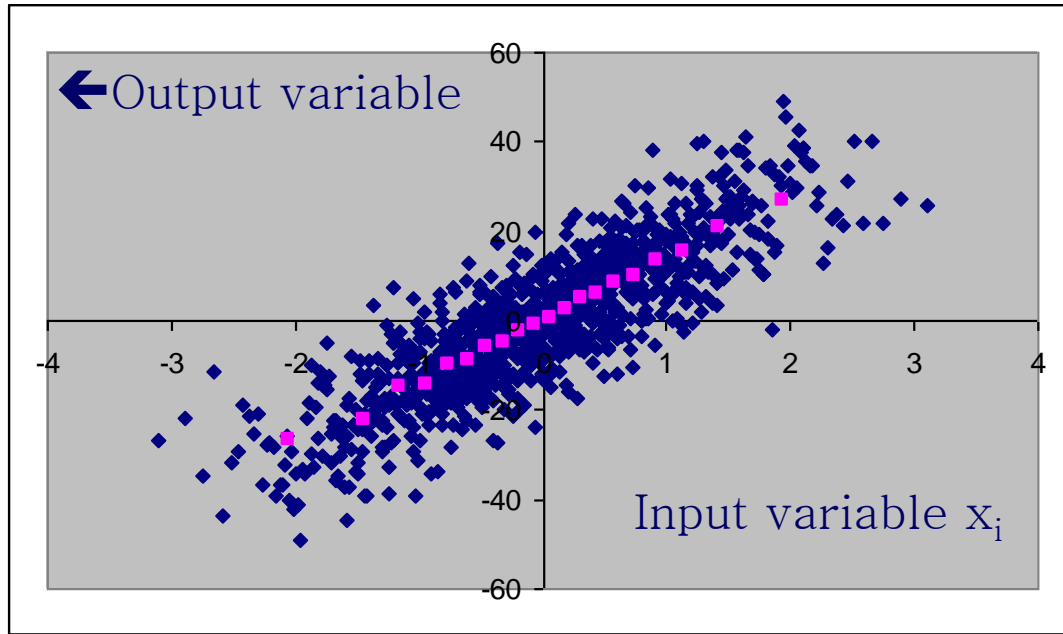


Each pink point is $\sim E_{\mathbf{X}_{\sim i}}(Y|X_i)$



Take the variance of
the pink points and
you have a
sensitivity measure

$$V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right)$$



Which factor
has the highest
 $V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right)$?

$$S_i \equiv \frac{V(E(Y|X_i))}{V_Y}$$

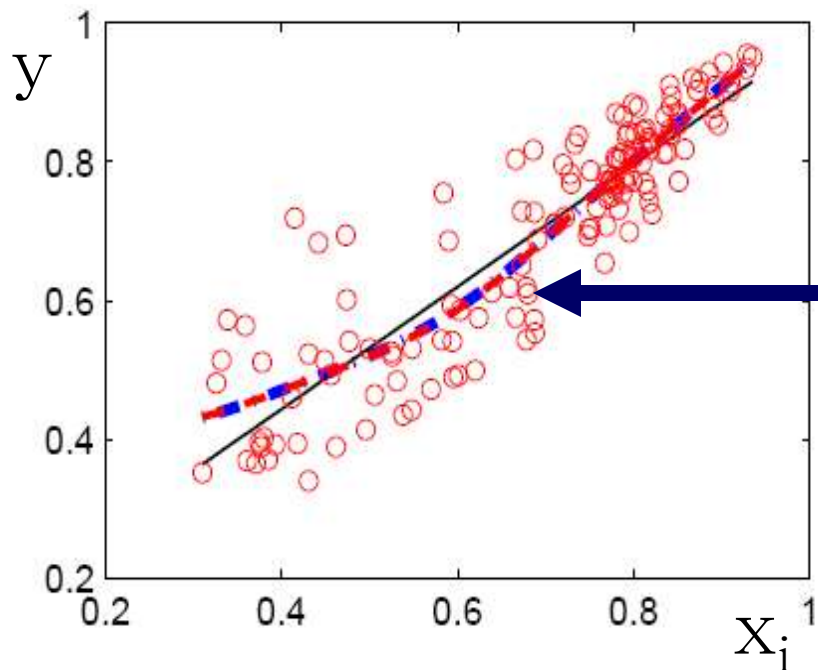
Pearson's correlation
ratio

Smoothed curve

$$S_i \equiv \eta_i^2 := \frac{V_{x_i} (\mathbf{E}_{\mathbf{x}_{\sim i}} (y \mid x_i))}{V(y)}$$

First order sensitivity index

Unconditional
variance



Smoothed curve:

$$\mathbf{E}_{\mathbf{x} \sim i} (y \mid x_i)$$

First order
sensitivity index:

$$\frac{V_{x_i} (\mathbf{E}_{\mathbf{x} \sim i} (y \mid x_i))}{V(y)}$$

$$V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right)$$

First order effect, or top marginal variance=

= the expected reduction in variance that would be achieved if factor X_i could be fixed.

Why?

Because:

$$V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right) + \\ + E_{X_i} \left(V_{\mathbf{X}_{\sim i}} (Y | X_i) \right) = V(Y)$$

Easy to prove using $V(Y) = E(Y^2) - E^2(Y)$

Because:

$$V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right) +$$

$+ E_{X_i} \left(V_{\mathbf{X}_{\sim i}} (Y | X_i) \right)$

 $= V(Y)$

This is what variance would be left (on average) if X_i could be fixed...

... then this ...



$$V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right) +$$
$$+ E_{X_i} \left(V_{\mathbf{X}_{\sim i}} (Y | X_i) \right) = V(Y)$$

... must be the expected reduction
in variance that would be achieved
if factor X_i could be fixed

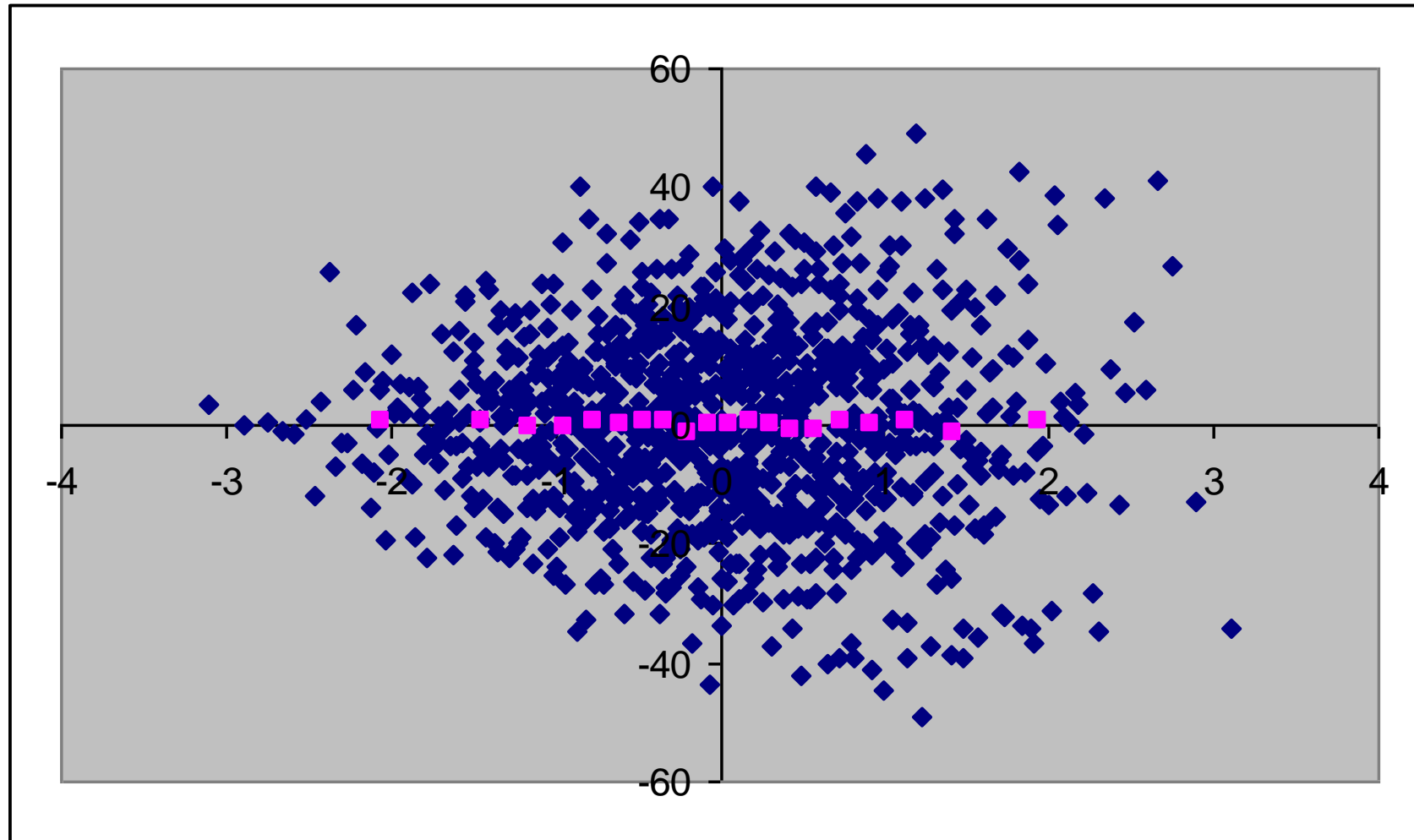
For additive models one can decompose the total variance as a sum of first order effects

$$\sum_i V_{X_i} \left(E_{\mathbf{X}_{\sim i}} (Y | X_i) \right) \approx V(Y)$$

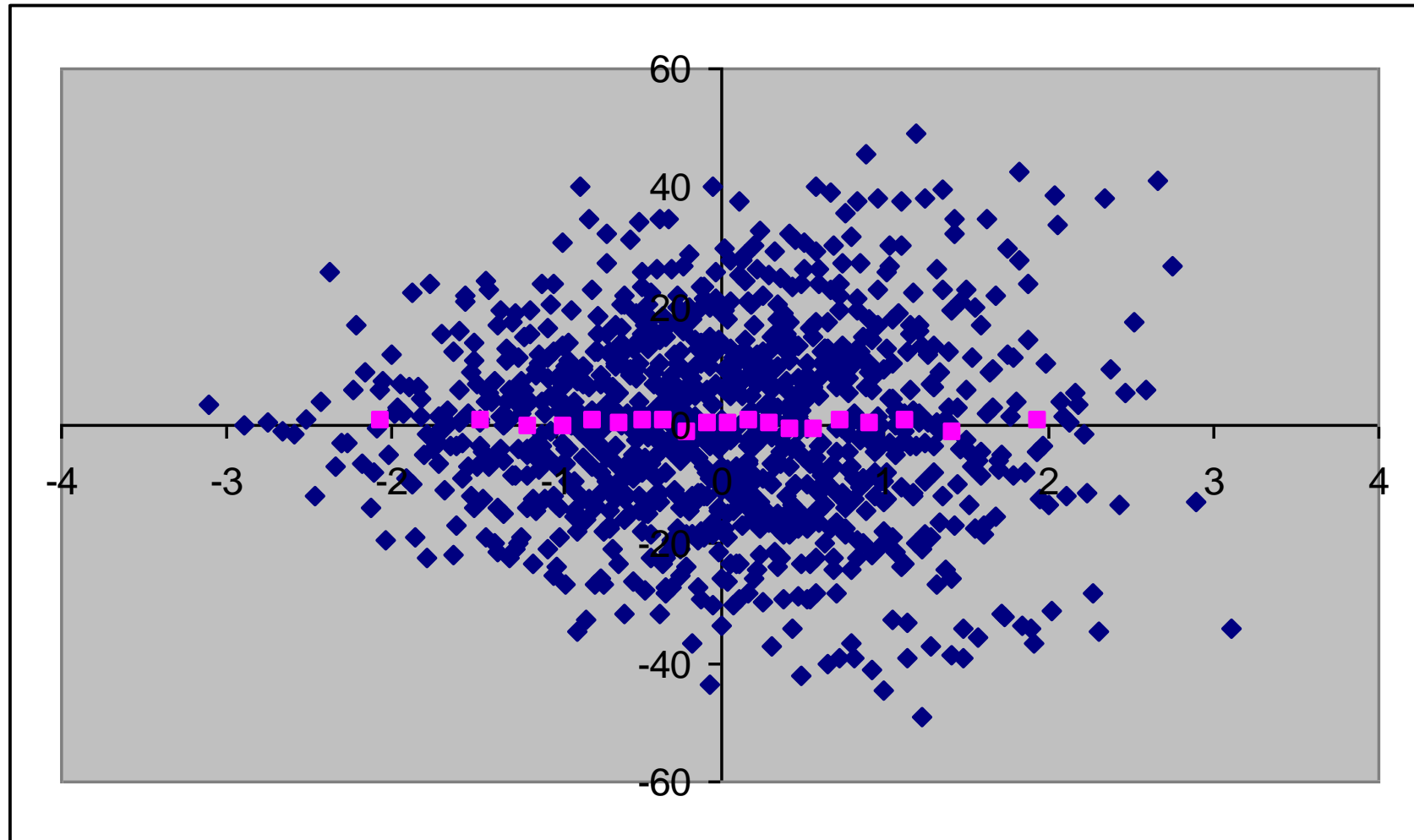
... which is also how additive models are defined

Non additive models

Is $S_i = 0$?



Is this factor non-important?



There are terms which capture two-way, three way, \dots interactions among variables.

All these terms are linked by a formula

Variance decomposition (ANOVA)

$$V(Y) =$$

$$\sum_i V_i + \sum_{i,j>i} V_{ij} + \dots + V_{123\dots k}$$

➔ Lesson Stefano Tarantola

EC impact assessment guidelines: sensitivity analysis & auditing

The screenshot shows the 'Better Regulation Guidelines' page on the European Commission website. The page features the European Commission logo and the title 'Better Regulation'. A navigation menu on the left includes links to Home, REFIT, Stakeholder consultations, Roadmaps / Inception Impact Assessments, Impact Assessment, Evaluation, Regulatory Scrutiny Board, and Guidelines. The 'Guidelines' section is expanded, showing links to 'Better Regulation Guidelines', 'Better Regulation "Toolbox"', and 'Key documents'. The main content area is titled 'Better Regulation Guidelines' and contains three paragraphs of text. The first paragraph explains that the guidelines explain what Better Regulation is and how it should be applied. The second paragraph states that they cover the whole policy cycle, from policy preparation to implementation and evaluation. The third paragraph notes that the guidelines are structured into chapters covering each instrument of the law-making process. Below the text are three links: 'Public consultation on the revision of the Commission's Impact Assessment Guidelines', 'Stakeholder Consultation Guidelines', and 'Consultation on the draft Commission Evaluation Policy Guidelines'. The right sidebar contains social media sharing options, a search bar, a 'Stay connected' section with links to Facebook, Twitter, and YouTube, a 'Latest documents' section with a link to '19/05/2015 - Better Regulation Package', and a 'Help us improve' section with a 'Find what you wanted?' survey and a 'Send' button. The footer of the page indicates the last update was on 11/09/2015 and provides links for legal notice, cookies, contact, and search.

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European Commission

Better Regulation

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REFIT
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Guidelines
Better Regulation Guidelines
Better Regulation "Toolbox"
Key documents

Better Regulation Guidelines

These guidelines explain what Better Regulation is and how it should be applied in the day to day practices when preparing new initiatives and proposals or managing existing policies and legislation.

They cover the whole policy cycle, from policy preparation and adoption to implementation and application, to evaluation and revision of EU law. For each of these phases there are a number of Better Regulation principles, objectives, tools and procedures to make sure that the EU has the best regulation possible. These relate to planning, impact assessment, stakeholder consultation, implementation and evaluation.

The [Better Regulation Guidelines](#) are structured into chapters which cover each of the instruments of the law-making process. The corresponding [toolbox](#) gives more detailed and technical information.

Better Regulation Guidelines are based on the outcomes of public consultation exercises carried out in 2013 and 2014.

- Public consultation on the revision of the Commission's Impact Assessment Guidelines
- Stakeholder Consultation Guidelines
- Consultation on the draft Commission Evaluation Policy Guidelines

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http://ec.europa.eu/smart-regulation/guidelines/docs/br_toolbox_en.pdf

Secrets of sensitivity analysis

Why should one
ever run a model
just once?

First secret: The most important question is the question.

Or: sensitivity analysis is not “run” on a model but on a model once applied to a question

Second secret: Sensitivity analysis should not be used to hide assumptions
[it often is]



Third secret: If sensitivity analysis shows that a question cannot be answered by the model one should find another question or model

[Often the love for one's own model prevails]

Badly kept secret:

There is always one more bug!

(Lubarsky's Law of Cybernetic Entomology)



And of course please don't run a sensitivity analysis where each factors has a 5% uncertainty



More than a technical
uncertainty and sensitivity
analysis?

1. Uncertainty and sensitivity analysis (never execute the model once)

2. Sensitivity auditing and quantitative storytelling (investigate frames and motivations)

Saltelli, A., Guimarães Pereira, Â., Van der Sluijs, J.P. and Funtowicz, S., 2013, 'What do I make of your latinorum? Sensitivity auditing of mathematical modelling', *Int. J. Foresight and Innovation Policy*, (9), 2/3/4, 213–234.

Saltelli, A., Does Modelling need a reformation? Ideas for a new grammar of modelling, available at <https://arxiv.org/abs/1712.06457>

3. Replace ‘model to predict and control the future’ with ‘model to help mapping ignorance about the future’ ...

... in the process exploiting and making explicit the metaphors embedded in the model

J. R. Ravetz, “Models as metaphors,” in Public participation in sustainability science : a handbook, and W. A. B. Kasemir, J. Jäger, C. Jaeger, Gardner Matthew T., Clark William C., Ed. Cambridge University Press, 2003, available at <http://www.nusap.net/download.php?op=getit&lid=11>

END



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