



# QUANTITATIVE STORYTELLING IN SOCIAL CONVERGENCE ANALYSIS

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# Presentation plan

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1. Introduction
2. The fortune of composite indicators
3. Quantitative story telling
4. Methodology
5. Research findings
  1. National vs. regional
  2. Different stakeholders
6. Conclusion
7. Further research

# Introduction

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- Can composite indicator tell more than one story?
- Convergence analysis
- Experiment:
  - Fixing the structure of CI while changing its scale,
  - Fixing its scale and changing the composition of its pillar

# The fortune of composite indicators

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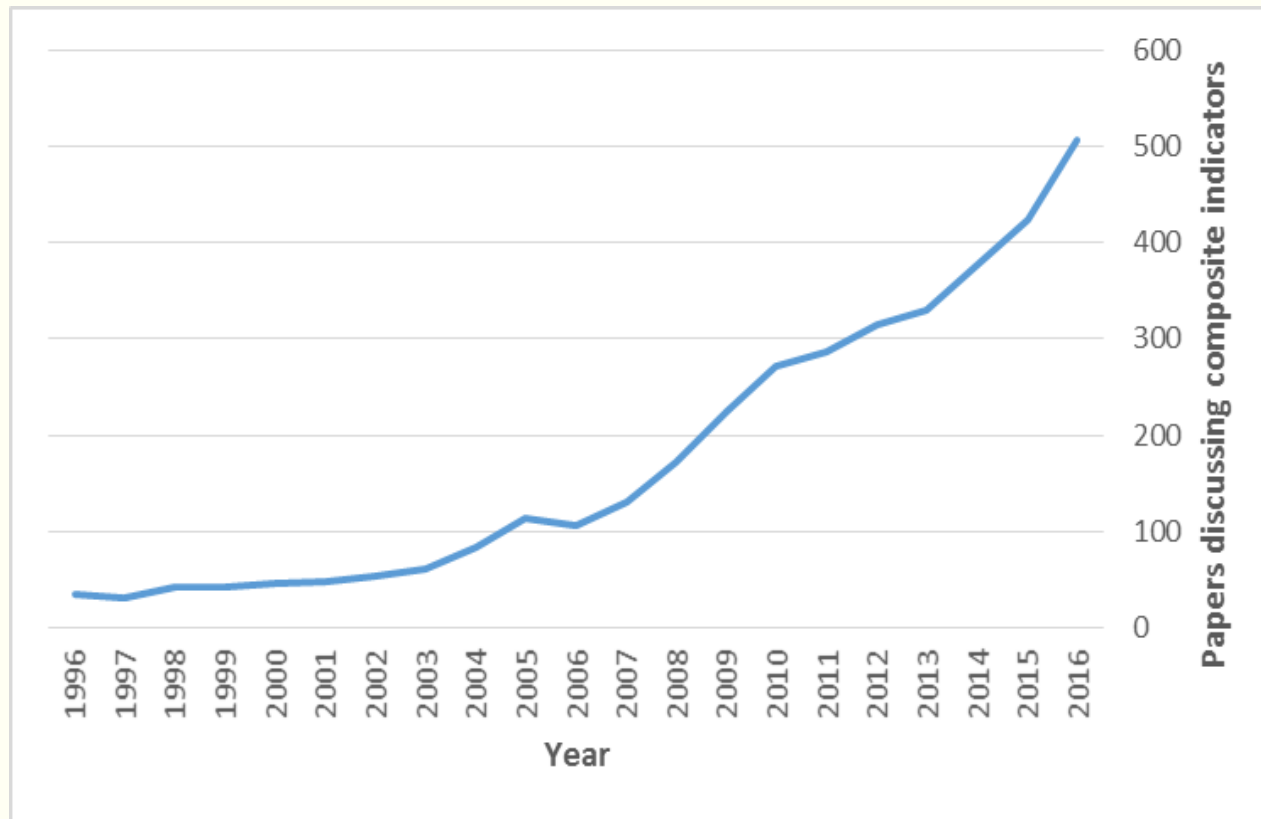


Figure 1, Search on [www.scopus.com](http://www.scopus.com) using as search string: TITLE-ABS-KEY("composite indicator\*") OR TITLE-ABS-KEY("composite index") OR TITLE-ABS-KEY("composite indices").

# The fortune of composite indicators

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- Composite indicators are very popular in analysis of:
  - Well-being
  - Communication technology development
  - Innovation
  - Health care system performance
  - Real estate market analysis
  - Countries/regions' competitiveness
  - Quality of institution
  - Sustainable development
  - Standard of living

New wave of CI – spatial composite indicators

# Pros of composite indicators

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- Can summarise complex, multi-dimensional realities with a view to supporting decision makers
- Are easier to interpret than a battery of many separate indicators
- Can assess progress of countries over time
- Reduce the visible size of a set of indicators without dropping the underlying information base
- Facilitate communication with general public
- Enable users to compare complex dimensions effectively

# Cons of composite indicators

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- May send misleading policy messages if poorly constructed or misinterpreted
- May invite simplistic policy conclusions
- May be misused – e.g. to support desired policy
- The selection of indicators and weight could be the subject of political dispute
- May lead to inappropriate policies if dimensions of performance that are difficult to measure are ignored
- May fall short in the context of policy analysis and negotiation, where different options and different ‘end in sight’ are relevant

# Two types of indices

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- According to Ravallion:
  - Those built on economic theory – direct monetary aggregates or based on shadow prices
  - ‘mashup indices’ – HDI, MPI



# Is a theory for composite indicators possible?

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- OECD-JRC handbook (2008) – 10 steps how to build CI
- Questionable weighting procedure (Becker et al. 2017; Paruolo et al., 2017)- sensitivity analysis?
- Conceptual streams:
  - Concept of democratization of expertise
  - Concept of extended peer community
  - Concept of social discovery
  - Sign – Object – Interpretant (S-O-I)

# Quantitative storytelling (QST)

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- Tautology that every measure of society corresponds to a frame
- EBP – evidence based policy
- QST – corresponds to different constituencies and social actors
- QST – broadening the spectrum of available frames
- OECD PISA study (Araujo et al., 2017; Saltelii, 2017)

# Methodology - CI

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- The classical approach to constructing composite indicators implies the assignment of variables to a given pillar (based on researchers' own knowledge or experts opinion), then aggregation of variables within the pillar, and finally the aggregation into a holistic composite indicator. In our paper we decided to follow that the most popular approach.

# Methodology - CI

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- Destimulants transformation:

$$x_{ijt}^s = \frac{1}{x_{ijt}}$$

- Normalization formula:

$$x'_{ijt} = \frac{x_{ijt}}{\max x_{ij,2005}}$$

# Methodology - CI

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- Composite indicator

$$CI_{it} = \frac{1}{p} \sum_{q=1}^p z_{iqt}$$

# Methodology – Beta-convergence

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- Beta convergence is a process in which countries with lower performance are improving faster than those with higher one (Sala-i- Martin, 1996).

$$g_i = a + b \log CI_{i,0} + \varepsilon_t$$

$$g_i = \frac{1}{T} \log \left( \frac{CI_{i,T}}{CI_{i,0}} \right)$$

# Methodology – Beta-convergence

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- The speed of convergence can be calculated according to formula (Barro, Sala-i-Martin, 2003):

$$\beta = -\frac{\ln(1 + b)}{T}$$

# Methodology – Sigma-convergence

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- As it was mentioned before the occurrence of beta-convergence is a necessary condition for sigma-convergence, however based on the same equation we can investigate the existence of sigma-divergence (Friedman, 1992; Quah, 1993). To do so the following linear trend model was estimated:

$$V_W = \alpha_0 + \alpha_1 t + \varepsilon_t$$

$$V_W = \frac{\sqrt{\sum_{i=1}^n (CI_i - CI)^2 \frac{l_i}{L}}}{CI}$$



# Research findings – same composites at different scales

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- EU countries vs. EU NUTS-2 regions
- Variables:
  - Employment rate
  - Households income in PPS per capita
  - Long term unemployment
  - Participation rate in education and training
  - NEET – young people neither in employment nor in education and training

# Research findings – I – beta-convergence

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- National:

|                      | coefficient    | standard error | p-value |
|----------------------|----------------|----------------|---------|
| const.               | 0.0165         | 0.0043         | 0.0007  |
| CI                   | <b>-0,0375</b> | 0.0101         | 0.0014  |
| R <sup>2</sup> =0.39 |                |                |         |

- Regional:

|                      | coefficient    | standard error | p-value |
|----------------------|----------------|----------------|---------|
| const.               | 0.0038         | 0.0015         | 0.0140  |
| CI                   | <b>-0.0099</b> | 0.0038         | 0.0140  |
| R <sup>2</sup> =0.25 |                |                |         |

Source: Authors' own study.

# Research findings – I – speed of convergence

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- National:

$$\beta = 0.35\%$$

- Regional:

$$\beta = 0.09\%$$

# Research findings – I – weighted C.V. dynamic

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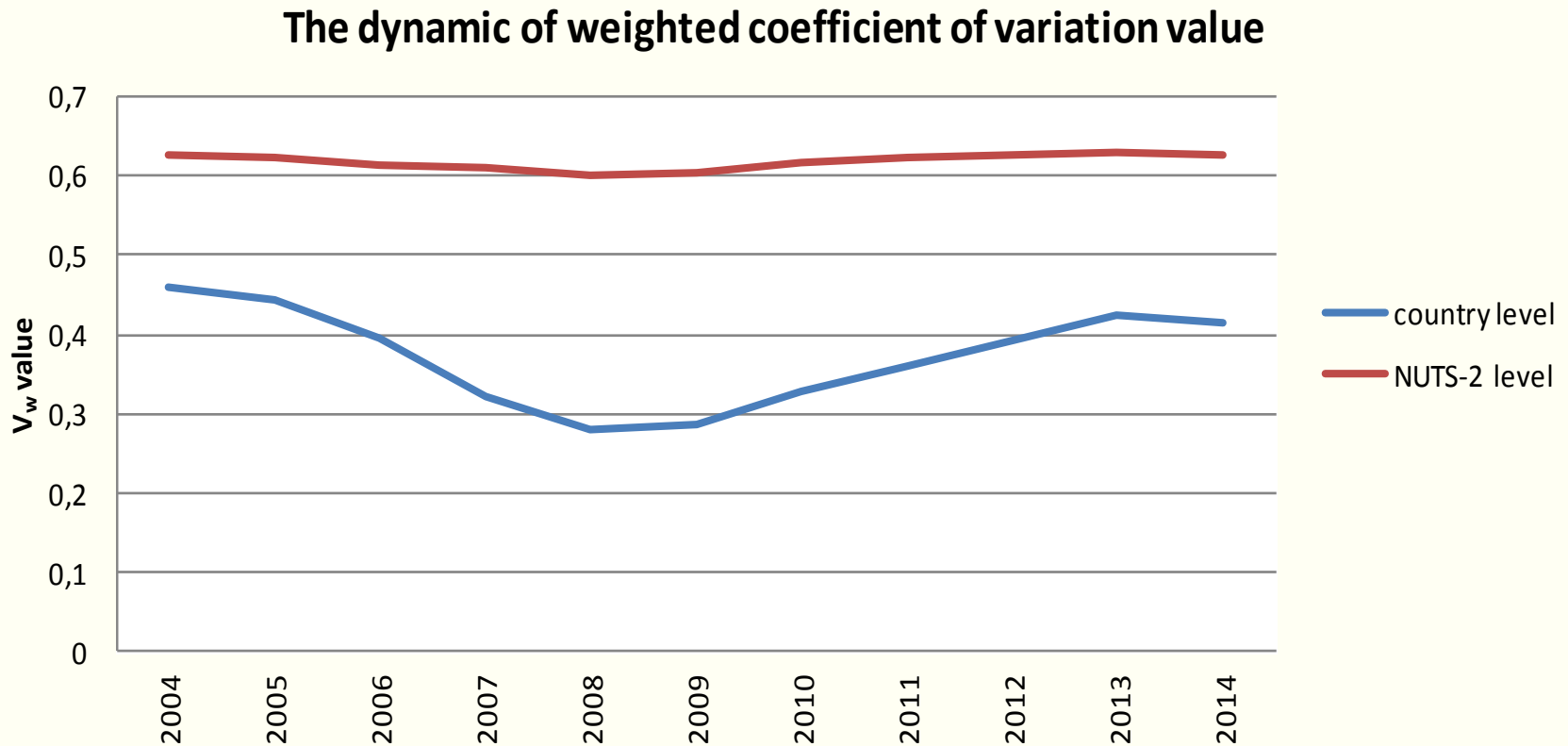


Figure 2. The dynamic of weighted coefficient of variation value.

Source: Authors' own study.

# Research findings – I – sigma convergence

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|               | $\alpha_0$        | $\alpha_1$          | $R^2$  |
|---------------|-------------------|---------------------|--------|
| country level | 0.3832<br>(0.000) | -0.0017<br>(0.7938) | 0.0178 |
| NUTS-2 level  | 0.6128<br>(0.000) | 0.0009<br>(0.3695)  | 0.0918 |

Source: Authors' own study.

# Research findings – I – within countries disproportions

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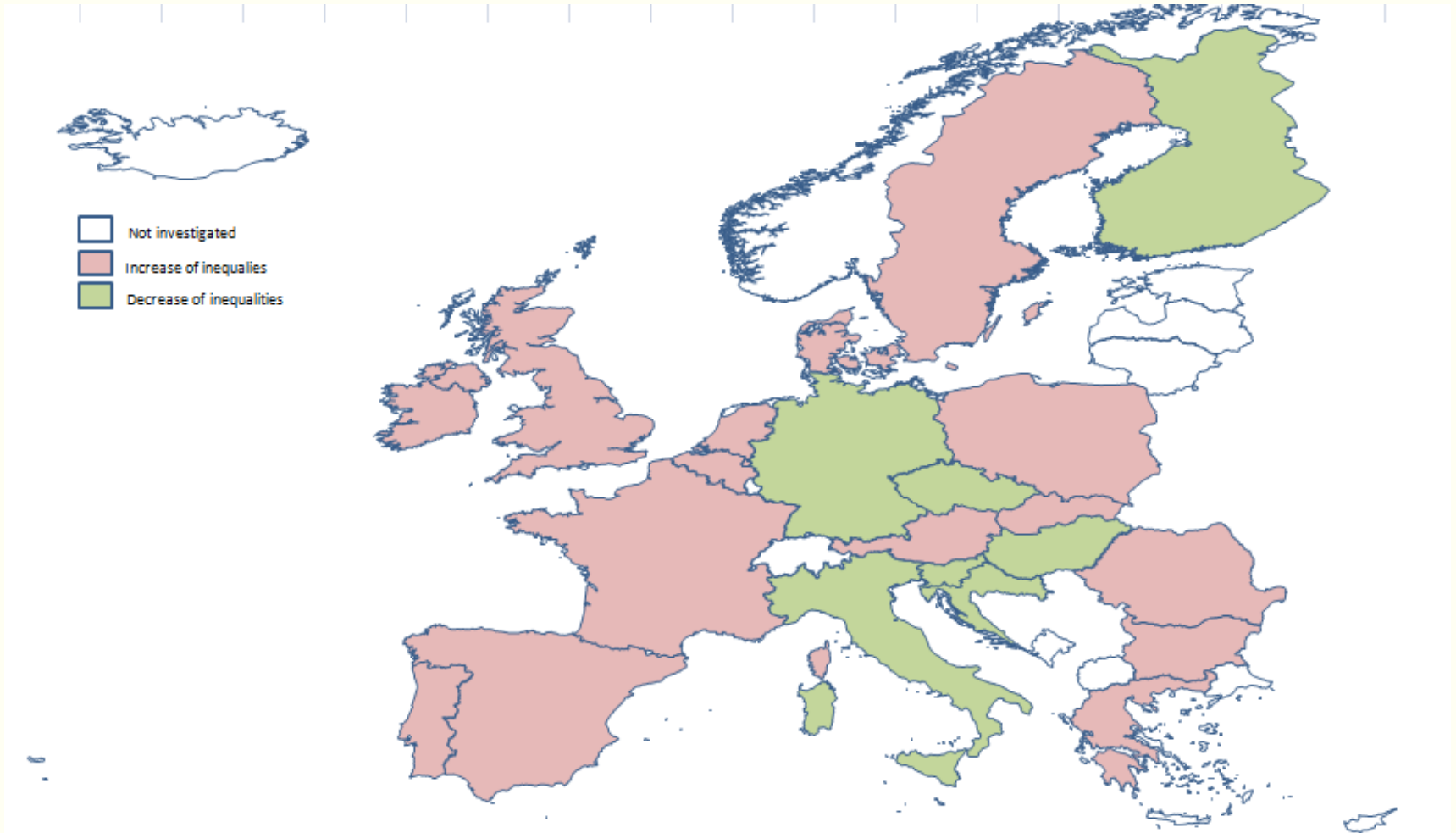
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| Convergence | Divergence        | No evidence    |
|-------------|-------------------|----------------|
| 1. Belgium  | 1. Denmark        | 1. Bulgaria    |
| 2. Germany  | 2. Greece         | 2. Czech Rep.  |
| 3. France   | 3. Spain          | 3. Ireland     |
| 4. Hungary  | 4. Croatia        | 4. Netherlands |
| 5. Austria  | 5. Italy          | 5. Poland      |
| 6. Slovakia | 6. Portugal       | 6. Finland     |
| 7. Sweden   | 7. Romania        |                |
|             | 8. Slovenia       |                |
|             | 9. United Kingdom |                |

Source: Authors' own study.

# Research findings – I – capital vs. other regions

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Source: Authors' own study.

# Research findings – Same scale different pillars

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| Stakeholder 1                                       | Stakeholder 2                                       | Stakohlder 3  | Stakholder 4  |
|---|---|---|---|
| 1. Opportunities and access to the labour market    | 1. Opportunities and access to the labour market    | 1. Opportunities and access to the labour market    | 1. Opportunities and access to the labour market    |
| 2. Dynamic labour market and fair working condition | 2. Dynamic labour market and fair working condition | 2. Dynamic labour market and fair working condition | 2. Dynamic labour market and fair working condition |
| 3. Public support/ Social protection and inclusion  | 3. Public support/ Social protection and inclusion  | 3. Public support/ Social protection and inclusion  | 3. Public support/ Social protection and inclusion  |
|   | 4. Governance / Fairness                            | 4. Functioning of health care                       | 4. Governance/ Fairness                             |
|   |   |   | 5. Functioning of health care                       |



## Research findings – II – Beta-convergence

| Stakeholder no.1       | coefficient | standard error | p-value |
|------------------------|-------------|----------------|---------|
| const.                 | 0.0009      | 0.0020         | 0.6430  |
| CI                     | -0.0093     | 0.0072         | 0.2050  |
| R <sup>2</sup> =0.2612 |             |                |         |
| Stakeholder no.2       | coefficient | standard error | p-value |
| const.                 | -0.0001     | 0.0018         | 0.9506  |
| CI                     | -0.0083     | 0.0064         | 0.2047  |
| R <sup>2</sup> =0.28   |             |                |         |
| Stakeholder no.3       | coefficient | standard error | p-value |
| const.                 | 0.0066      | 0.0036         | 0.0813  |
| CI                     | 0.0022      | 0.0122         | 0.8572  |
| R <sup>2</sup> =0.12   |             |                |         |
| Stakeholder no.4       | coefficient | standard error | p-value |
| const.                 | 0.0034      | 0.0028         | 0.2394  |
| CI                     | -0.0038     | 0.0093         | 0.6842  |
| R <sup>2</sup> =0.25   |             |                |         |

Source: Authors' own study.

# Research findings – II – CI C.V. dynamic

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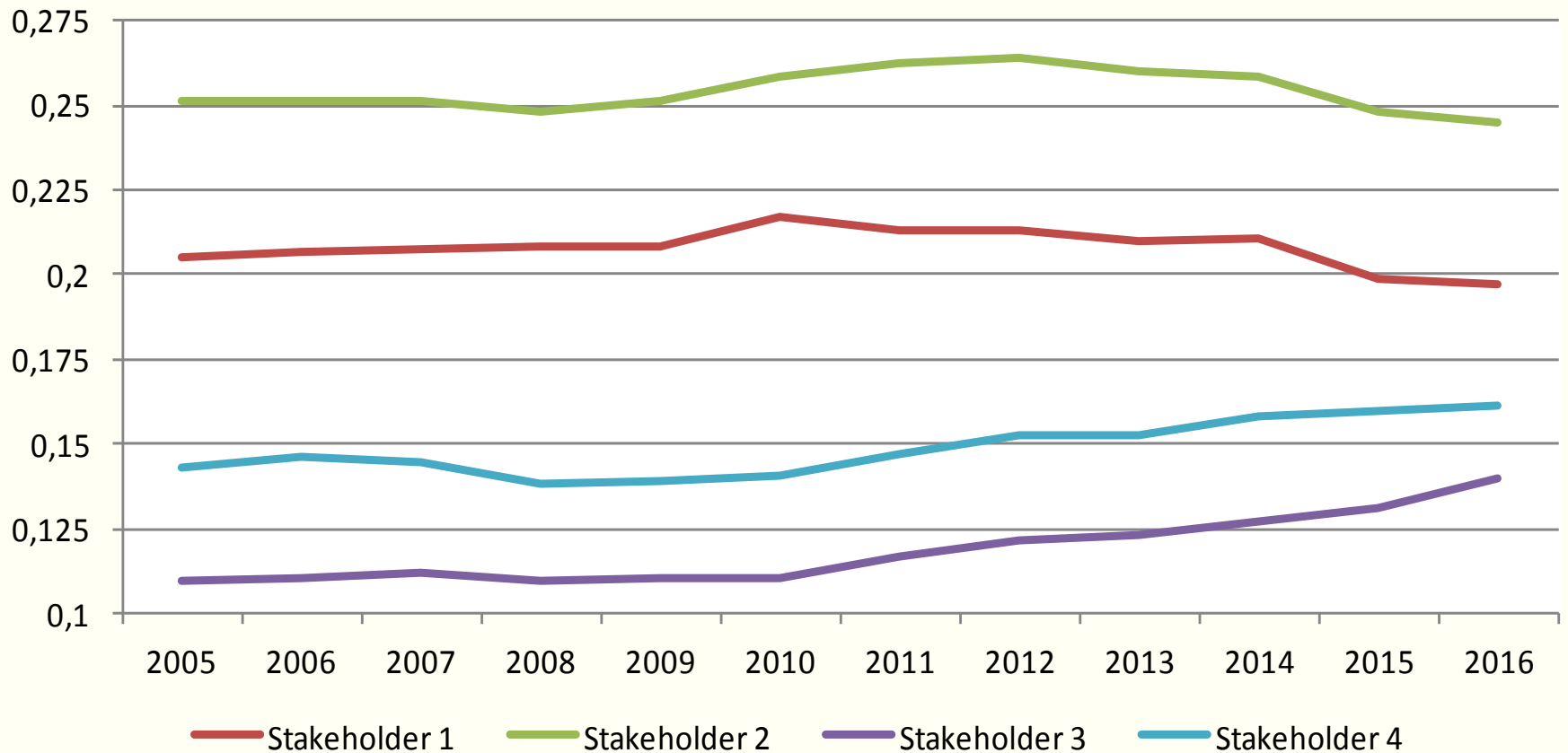


Figure 3. The dynamic of coefficient of variation of CI value.

Source: Authors' own study.

## Research findings – II– sigma convergence

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|               | $\alpha_0$      | $\alpha_1$             | R <sup>2</sup> |
|---------------|-----------------|------------------------|----------------|
| Stakeholder 1 | 0.2150 (0.0000) | -0.0004 (0.4234)       | 0.2649         |
| Stakeholder 2 | 0.2531 (0.0000) | 0.0001 (0.7551)        | 0.2128         |
| Stakeholder 3 | 0.1019 (0.0000) | <b>0.0025 (0.0000)</b> | 0.8403         |
| Stakeholder 4 | 0.1360 (0.0000) | <b>0.0020 (0.0006)</b> | 0.7125         |

Source: Authors' own study.

# Conclusions

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- Modification of philosophy of CI
- Cohesion policy offers a convenient battleground to test this methodology
- Is countries convergence more important than regional or within-country?
- Should fairness be targeted by a cohesion policy?
- Should health care be targeted by a cohesion policy?

# Further research

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- Refining the analysis with more data
- Rebalancing weights to their target importance using SA
- Dynamic spatial panel model



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THANK YOU

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